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## **Two approaches for directional overcurrent relays coordination in interconnected power systems with distributed generation**

By

Saadoun Abd ElAziz Mostafa<sup>\*</sup>, Doaa khalil Ibrahim<sup>\*\*</sup>, Essam El-Din Abo El-Zahab<sup>\*\*</sup>

### **Abstract:**

Connection of distributed generation (DGs) powered by renewable energy resources in power systems has numerous benefits. However the presence of these (DGs) increase the fault current levels in different points, and disturb the protection coordination of the existing relays. Two approaches are proposed for coordination of directional overcurrent relays (DOCRs) in power systems with (DGs), depending on the types of system relays either adaptive or non adaptive.

For adaptive protection system, the first proposed approach is based on linear programming technique which used to calculate the relay settings in case of DGs existing or not. For non-adaptive protection system, the second proposed approach is introduced, in which minimum impedance of fault current limiter is calculated to restore the coordination of relays without altering the original relay settings. The two proposed approaches are implemented and tested on IEEE-39 bus test system.

**Keywords:** Distributed Generation, Fault Current Limiter, Relay Setting, Relays Coordination.

<sup>\*</sup> Arab Contractor Company, Egypt

<sup>\*\*</sup> Faculty of Engineering, Cairo University, Egypt

## **1. Introduction:**

The advantageous applications of DG can be summarized as: backup generation, loss reduction, power quality improvement, grid expansion postponement, rural and remote application, combined heat and power generation, and financial and trading purposes[1]. These advantages can be achieved if the relevant issues are deliberately taken into account. One of the most influential issues is the coordination of protective devices.

The presence of DG tends to negatively affect protective relays coordination. The unacceptable operation of protective devices may occur, since the protection coordination will be lost if the fault current characteristic flowing through any protective device is changed, especially in case of directional overcurrent relays (DOCRs). In power delivery systems without DGs, several methods are proposed for the coordination of these relays. Traditionally, a trial and error procedure was employed for setting relays in multi-loop networks. In a trial to minimize the number of iterations needed for coordination process, a technique is proposed to break all the loops at the breakpoints and locate the relays for which to start the coordination procedure [2]. A systematic approach for determining the relative sequence setting of the relays in a multi-loop network based on a linear graph theory approach is suggested in [3]. The graph theoretic concepts are extended by proposing a systematic algorithm for determining a relative sequence matrix corresponding to a set of sequential pairs which reduced the number of iterations [4]. A functional dependency concept for topological analysis of the protection scheme is proposed by expressing the constraints on the relay settings through a set of functional dependencies [5]. Both the graph theoretic and functional dependency approaches provide a solution which is the best setting, but not necessarily an optimal solution.

The coordination of DOCRs in optimization frame is presented in [6] by using generalized reduced gradient nonlinear optimization technique. Another method is proposed to consider the dynamic changes in the networks topology for DOCRs using linear programming [7].

In some other researches, coordination problem has been solved in the frame of optimization techniques such as, Genetic algorithm (GA), Evolutionary algorithm (EA), and particle swarm optimization. A modified particle swarm optimization method is proposed for optimal DOCRs settings taking into account the discrete values for the pick-up current settings by formulating coordination problem as a mixed integer nonlinear problem [8]. A method based on GA was developed to solve the problems of miscoordination and continuous or discrete time setting multipliers [9].

In this paper, the problems of DOCRs coordination in power system network including DG in case of either adaptive or non adaptive protection system relays types are solved

using two proposed solutions. DOCRs coordination is stated as a linear programming optimization problem using the first proposed approach. However the second approach involves the implementation of a fault current limiter to locally limit the DG fault current, and thus restore the original relay coordination. The implementation of the two approaches based on IEEE-39 bus case study is carried out.

## **2. Overview on Linear Programming:**

Linear programming (LP) is a technique for optimization problems. In such problems, a linear objective function is subject to linear equality and inequality constraints. A linear programming problem may be defined as the problem of maximizing or minimizing a linear function subject to linear constraints. Not all linear programming problems are so easily solved. There may be many variables and many constraints. Some variables may be constrained to be nonnegative and others unconstrained. Some of the main constraints may be equalities and others inequalities.

DOCRs coordination problem can be defined as linear programming problem with constraints and can be solved using one of the linear programming techniques, namely: simplex, dual simplex, or two phase simplex technique.

The simplex algorithm, invented by George Dantzig in 1947, is one of the earliest and best known optimization algorithms for obtaining a basic feasible solution; if the solution is not optimal, the method provides for finding a neighboring basic feasible solution that has a lower or equal value of function. The process is repeated until, in a finite number of steps, an optimum is found.

Dual simplex method is a variant of regular simplex method, developed by Lemke, to solve a linear programming problem. It starts from infeasible solution to the primal. The method works in an iterative manner such that it forces the solution to become feasible as well as optimal at some stage. This method has some important characteristics: it does not require the phase I calculations of the two phase simplex method. This is a desirable feature, as the starting point obtained at the end of phase I, may not be near optimal. In addition, it works towards feasibility and optimality simultaneously; the solution is expected to be achieved in less number of iterations [10].

Many software have been developed for the mentioned various linear programming techniques, optimization toolbox included in Matlab environment is considered an easy and powerful tool to implement different linear programming techniques.

## **3- Overview on Relay Characteristics:**

A typical inverse time overcurrent has two values to be set, the pick-up current value ( $I_p$ ) which is the minimum current value for which the relay operates, and the time dial

setting ( $TDS$ ) which defines the operation time of the device for each current value. Under simplistic assumptions, the relay characteristics are assumed identical and with characteristic functions approximated by:

$$t_{i,k} = \frac{0.14 \times TDS_i}{\left(\frac{I_{i,k}}{I_{Pi}}\right)^{0.02} - 1} \quad (1)$$

Where:

$I_{i,k}$  is the short circuit current passing through the relay  $R_i$ , for fault at  $k$ ,

$t_{i,k}$  is the operating time of the relay  $R_i$ , for fault at  $k$ ,

#### **4. First Proposed Approach Programming:**

##### **4.A. Coordination Problem Formulation:**

The problem of DOCRs coordination is stated here as a linear programming optimization problem using the first proposed approach. Solving this problem implies finding the coordinated settings  $TDS$  and pick-up current setting for all the directional overcurrent relays in the system so that the sum of operating times of the primary relays for near end faults is minimized and the coordination constraints are satisfied.

Therefore:

- The objective function is that the total time for  $N$  primary relays for near end fault is

minimized ( $\sum_{i=1}^N t_i$  is minimum).

- To ensure relay coordination, the operating time of the backup relay has to be greater than that of the primary relay for the same fault location by a coordination time interval as :  $t_{j,i} - t_i \geq CTI_{j,i}$

Where:  $t_{j,i}$  is the operation time of the first back up  $j$  <sup>th</sup> relay for a near end fault at the  $i$  <sup>th</sup> relay,  $CTI_{j,i}$  is the coordination time interval for backup-primary relay pair  $(j,i)$ . It can be chosen based on the local distribution company practice, which consists of: relay overtravel time, the breaker operating time, and safety margin for relay error. It can take a value between 0.2 and 0.5 s. In this paper, a coordination time interval of 0.2 s was adopted.

- The boundary conditions on relay settings can be written as linear inequalities, of two sets as follows:

$$TDS_{i,\min} \leq TDS_i \leq TDS_{i,\max}, \quad Ip_{i,\min} \leq Ip_i \leq Ip_{i,\max}$$

Where:

$TDS_{i,\min}$ ,  $TDS_{i,\max}$  is minimum and maximum value of  $TDS$  of relay  $R_i$  respectively.  $TDS_{i,\min}$ ,  $TDS_{i,\max}$  are taken 0.05 and 1.1 respectively.

$Ip_i$  is the pickup current settings of relay  $R_i$ . Limits of  $Ip_i$  are chosen between 1.25 and 2 times the maximum load current seen by each relay.

For previously predefined value of  $Ip_i = Ip_{Fixed}$ , Equation (1) can be reduced to:

$$t_{i,k} = a_{i,k} * TDS_i \quad (2)$$

Therefore, the problem of DOCRs Coordination could be treated as a LP problem.

#### **4.B. DOCRs Coordination for a Power System Configuration Without DG:**

To test the first proposed method, the case study of IEEE-39 bus system that shown in Figure (1) is simulated. This case study system has 345, 230 & 22 kV buses, with 34 lines, 10 generators, 12 transformers and 84 OC relays.

Firstly, load flow and near-end fault primary and backup relays currents are calculated.

Then, the optimization model is formulated as a linear programming (LP) problem considering previously predetermined values of  $Ip$  which varies between 1.25 and 2 times the maximum load current seen by each relay and  $TDS$  lies between 0.05 and 1.1.

For a fixed  $Ip$  corresponding to 1.5 times maximum load current and 1.5A for relays in the opposite direction,  $TDS$  values are calculated for each relay and coordination time interval (CTI) constraints are checked, if the constraints are violated, another values of  $Ip$  is chosen. The above steps are shown in Figure (2).

By applying the above procedure, all constraints are satisfied. Tables (1) and (2) demonstrate the obtained results for testing the first approach.

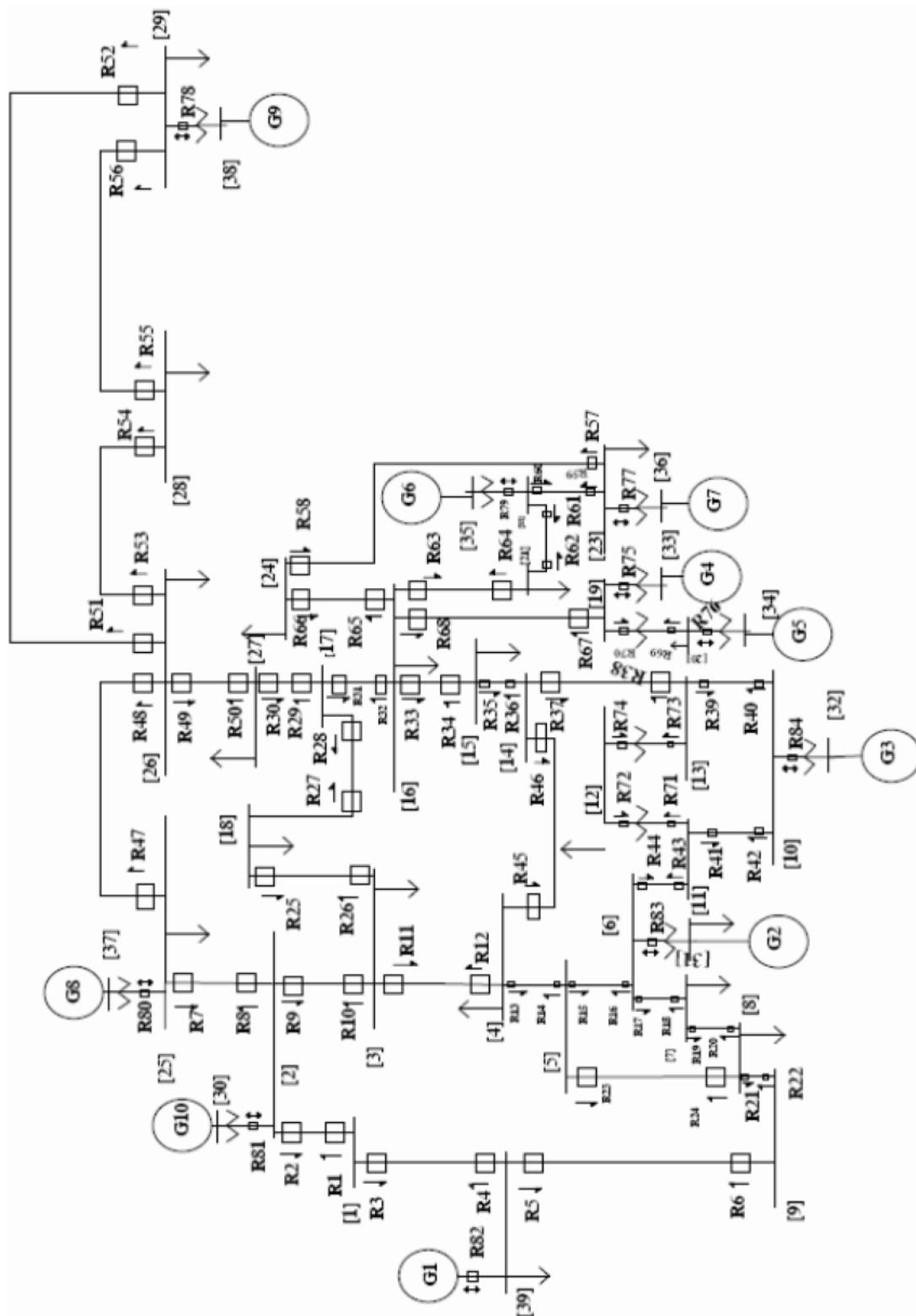
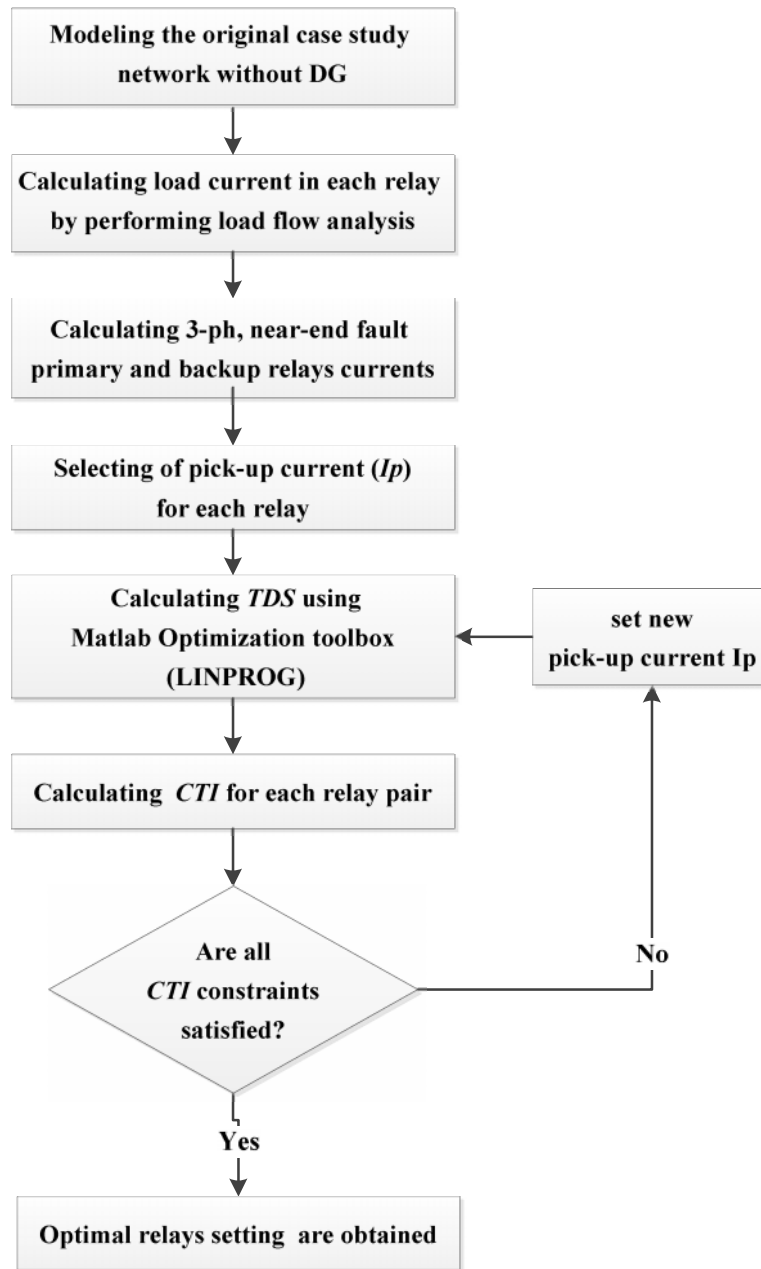


Figure (1): IEEE-39 bus system



**Figure (2):** Flow chart of DOCRs coordination in a power system configuration without DG using first approach

**Table (1):** *Ips for relays in power system configuration without DG*

<i>Ip</i>	Value	<i>Ip</i>	Value	<i>Ip</i>	Value	<i>Ip</i>	Value
<i>Ip1</i>	1.5	<i>Ip22</i>	2.203125	<i>Ip43</i>	10.72125	<i>Ip64</i>	10.08
<i>Ip2</i>	3.78	<i>Ip23</i>	10.0875	<i>Ip44</i>	1.5	<i>Ip65</i>	1.5
<i>Ip3</i>	3.658125	<i>Ip24</i>	1.5	<i>Ip45</i>	1.5	<i>Ip66</i>	3.03375
<i>Ip4</i>	1.5	<i>Ip25</i>	1.063125	<i>Ip46</i>	8.2575	<i>Ip67</i>	5.478
<i>Ip5</i>	1.771875	<i>Ip26</i>	1.5	<i>Ip47</i>	2.334375	<i>Ip68</i>	1.5
<i>Ip6</i>	1.5	<i>Ip27</i>	1.5	<i>Ip48</i>	1.5	<i>Ip69</i>	1.5
<i>Ip7</i>	7.57125	<i>Ip28</i>	5.848125	<i>Ip49</i>	8.255625	<i>Ip70</i>	5.229375
<i>Ip8</i>	1.5	<i>Ip29</i>	1.344375	<i>Ip50</i>	1.5	<i>Ip71</i>	1.333125
<i>Ip9</i>	11.25188	<i>Ip30</i>	1.5	<i>Ip51</i>	1.5	<i>Ip72</i>	1.5
<i>Ip10</i>	1.5	<i>Ip31</i>	1.5	<i>Ip52</i>	6.0825	<i>Ip73</i>	1.460625
<i>Ip11</i>	4.12875	<i>Ip32</i>	6.395625	<i>Ip53</i>	1.5	<i>Ip74</i>	1.5
<i>Ip12</i>	1.5	<i>Ip33</i>	9.84375	<i>Ip54</i>	4.5375	<i>Ip75</i>	7.545
<i>Ip13</i>	1.5	<i>Ip34</i>	1.5	<i>Ip55</i>	1.5	<i>Ip76</i>	9.85725
<i>Ip14</i>	5.098125	<i>Ip35</i>	1.5	<i>Ip56</i>	10.5	<i>Ip77</i>	6.71475
<i>Ip15</i>	1.5	<i>Ip36</i>	1.60125	<i>Ip57</i>	10.62563	<i>Ip78</i>	9.9045
<i>Ip16</i>	6.036	<i>Ip37</i>	1.5	<i>Ip58</i>	1.5	<i>Ip79</i>	7.97625
<i>Ip17</i>	5.42775	<i>Ip38</i>	9.163125	<i>Ip59</i>	1.5	<i>Ip80</i>	6.4335
<i>Ip18</i>	1.5	<i>Ip39</i>	1.5	<i>Ip60</i>	1.790625	<i>Ip81</i>	8.446875
<i>Ip19</i>	6.013125	<i>Ip40</i>	9.4125	<i>Ip61</i>	7.374	<i>Ip82</i>	12.23303
<i>Ip20</i>	1.5	<i>Ip41</i>	1.5	<i>Ip62</i>	1.5	<i>Ip83</i>	7.15425
<i>Ip21</i>	1.5	<i>Ip42</i>	10.9425	<i>Ip63</i>	1.5	<i>Ip84</i>	8.13525



**Table (2): Optimal TDS for relays in power system configuration without DG**

TDS	Value	TDS	Value	TDS	Value	TDS	Value
TDS1	0.529579	TDS22	0.435473	TDS43	0.232433	TDS64	0.132519
TDS2	0.3093571	TDS23	0.235767	TDS44	0.730852	TDS65	0.486888
TDS3	0.2479933	TDS24	0.472817	TDS45	0.656957	TDS66	0.35082
TDS4	0.6414664	TDS25	0.672985	TDS46	0.304848	TDS67	0.186422
TDS5	0.5701535	TDS26	0.752233	TDS47	0.529214	TDS68	0.05
TDS6	0.3763307	TDS27	0.645655	TDS48	0.519719	TDS69	0.484394
TDS7	0.2933137	TDS28	0.463591	TDS49	0.31609	TDS70	0.05
TDS8	0.664837	TDS29	0.678976	TDS50	0.551281	TDS71	0.05
TDS9	0.3401322	TDS30	0.565973	TDS51	0.284946	TDS72	0.272794
TDS10	0.6142968	TDS31	0.637003	TDS52	0.109759	TDS73	0.05
TDS11	0.4520729	TDS32	0.467611	TDS53	0.286098	TDS74	0.27674
TDS12	0.6751627	TDS33	0.393544	TDS54	0.167761	TDS75	0.109318
TDS13	0.4968642	TDS34	0.574515	TDS55	0.205804	TDS76	0.05
TDS14	0.4139164	TDS35	0.639737	TDS56	0.130258	TDS77	0.074992
TDS15	0.3335647	TDS36	0.657129	TDS57	0.169382	TDS78	0.05
TDS16	0.2473283	TDS37	0.669728	TDS58	0.362934	TDS79	0.081285
TDS17	0.2126053	TDS38	0.28067	TDS59	0.348031	TDS80	0.092618
TDS18	0.3122686	TDS39	0.579341	TDS60	0.381494	TDS81	0.29632
TDS19	0.2736297	TDS40	0.319667	TDS61	0.107456	TDS82	0.345324
TDS20	0.5298683	TDS41	0.634601	TDS62	0.303883	TDS83	0.064807
TDS21	0.466287	TDS42	0.267072	TDS63	0.516804	TDS84	0.073465

#### **4.C. DOCRs Miscoordination in a Power System Configuration with DG:**

DG is assumed to be added at bus 28, the transient reactance and capacity of the DG are 0.02 pu and 10 MVA respectively. The DG is connected to the network through a transformer of 10 MVA capacity and 0.01 pu reactance. The near-end fault primary and backup relays current are calculated in the presence of DG. Table (3) shows miscoordination occurrence cases for 19 pair of relays as the coordination time intervals are less than 0.2 sec

**Table (3):** Miscoordination in a power system configuration with DG

<i>CTI</i>	value	<i>CTI</i>	value
<i>CTI</i> 10,8	0.1984	<i>CTI</i> 49,30	0.1795
<i>CTI</i> 48,7	0.1926	<i>CTI</i> 28,25	0.1979
<i>CTI</i> 54,48	0.1485	<i>CTI</i> 9,26	0.1961
<i>CTI</i> 52,48	0.1901	<i>CTI</i> 46,12	0.1989
<b><i>CTI</i> 54,49</b>	<b>0.0159</b>	<i>CTI</i> 11,45	0.1983
<i>CTI</i> 52,49	0.0543	<i>CTI</i> 72,41	0.1988
<i>CTI</i> 7,9	0.1903	<i>CTI</i> 33,35	0.1989
<i>CTI</i> 25,10	0.1984	<i>CTI</i> 30,31	0.1883
<i>CTI</i> 51,56	0.1961	<i>CTI</i> 31,33	0.1963
<i>CTI</i> 55,52	0.1642		

#### **4.D. DOCRs Coordination in a Power System Configuration with DG:**

Load flow and near-end fault primary and backup relays current are calculated in the presence of DG using (LP) technique. For a fixed  $I_p$ ,  $TDS$  values are calculated for each relay, then coordination time interval ( $CTI$ ) constraints are checked, if the constraints are violated, another value of  $I_p$  is chosen till all constraints satisfied.

The above steps are the same as described in Figure (2). Therefore, by applying the above procedure, the all constraints (143) for the studied network with DG are satisfied.

Tables (4) and (5) demonstrate the obtained results for testing the first approach.

**Table (4):** Optimal TDS for relays in power system configuration with DG using first proposed approach

TDS	Value	TDS	Value	TDS	Value	TDS	Value
TDS1	0.5289336	TDS22	0.4358532	TDS43	0.2320537	TDS64	0.1324828
TDS2	0.3082957	TDS23	0.2363354	TDS44	0.7324193	TDS65	0.4873489
TDS3	0.2471482	TDS24	0.4737728	TDS45	0.6579499	TDS66	0.3504673
TDS4	0.6408254	TDS25	0.6665916	TDS46	0.3050039	TDS67	0.1862339
TDS5	0.5694809	TDS26	0.7528269	TDS47	0.5342886	TDS68	0.05
TDS6	0.376151	TDS27	0.6461303	TDS48	0.5269608	TDS69	0.483984
TDS7	0.2941975	TDS28	0.4630452	TDS49	0.3217389	TDS70	0.05
TDS8	0.6642149	TDS29	0.6828945	TDS50	0.5495256	TDS71	0.05
TDS9	0.3403531	TDS30	0.5731229	TDS51	0.2985431	TDS72	0.2736158
TDS10	0.6146338	TDS31	0.6397358	TDS52	0.1243865	TDS73	0.05
TDS11	0.4512626	TDS32	0.4690496	TDS53	0.298911	TDS74	0.2770615
TDS12	0.6752644	TDS33	0.3931753	TDS54	0.1951805	TDS75	0.109225
TDS13	0.4979912	TDS34	0.5743806	TDS55	0.239716	TDS76	0.05
TDS14	0.4182135	TDS35	0.640649	TDS56	0.1383463	TDS77	0.0749863
TDS15	0.3344074	TDS36	0.6643197	TDS57	0.169308	TDS78	0.05
TDS16	0.2492072	TDS37	0.6705945	TDS58	0.3632686	TDS79	0.0812488
TDS17	0.2134017	TDS38	0.2825611	TDS59	0.3481035	TDS80	0.092531
TDS18	0.3129088	TDS39	0.5801126	TDS60	0.3814084	TDS81	0.2958481
TDS19	0.2748826	TDS40	0.3215791	TDS61	0.1074561	TDS82	0.3450451
TDS20	0.5307297	TDS41	0.636165	TDS62	0.3041644	TDS83	0.0668114
TDS21	0.4661235	TDS42	0.2666553	TDS63	0.517168	TDS84	0.0736228

**Table (5): CTI of all relay pairs in power system configuration with DG using first approach**

<i>CTI<sub>j,i</sub></i>	<i>CTI</i>	<i>CTI<sub>j,i</sub></i>	<i>CTI</i>	<i>CTI<sub>j,i</sub></i>	<i>CTI</i>	<i>CTI<sub>j,i</sub></i>	<i>CTI</i>
<i>CTI<sub>4,1</sub></i>	0.2	<i>CTI<sub>27,29</sub></i>	0.304798	<i>CTI<sub>72,41</sub></i>	0.2	<i>CTI<sub>67,33</sub></i>	0.274007
<i>CTI<sub>7,2</sub></i>	0.651483	<i>CTI<sub>26,27</sub></i>	0.2	<i>CTI<sub>39,42</sub></i>	0.2	<i>CTI<sub>36,34</sub></i>	0.2
<i>CTI<sub>10,2</sub></i>	0.62814	<i>CTI<sub>21,6</sub></i>	0.2	<i>CTI<sub>84,42</sub></i>	0.270574	<i>CTI<sub>17,19</sub></i>	0.2
<i>CTI<sub>81,2</sub></i>	0.634968	<i>CTI<sub>28,25</sub></i>	0.2	<i>CTI<sub>18,44</sub></i>	0.2	<i>CTI<sub>22,20</sub></i>	0.2
<i>CTI<sub>1,8</sub></i>	0.2	<i>CTI<sub>9,26</sub></i>	0.2	<i>CTI<sub>83,44</sub></i>	0.2	<i>CTI<sub>23,20</sub></i>	0.2
<i>CTI<sub>10,8</sub></i>	0.2	<i>CTI<sub>12,26</sub></i>	0.2	<i>CTI<sub>43,17</sub></i>	0.524621	<i>CTI<sub>19,21</sub></i>	0.248228
<i>CTI<sub>81,8</sub></i>	0.2	<i>CTI<sub>82,4</sub></i>	0.2	<i>CTI<sub>15,17</sub></i>	0.2	<i>CTI<sub>23,21</sub></i>	0.331628
<i>CTI<sub>48,7</sub></i>	0.2	<i>CTI<sub>6,4</sub></i>	0.2	<i>CTI<sub>83,17</sub></i>	0.717138	<i>CTI<sub>19,24</sub></i>	0.2
<i>CTI<sub>80,7</sub></i>	0.2	<i>CTI<sub>82,5</sub></i>	0.263332	<i>CTI<sub>20,18</sub></i>	0.2	<i>CTI<sub>22,24</sub></i>	0.278113
<i>CTI<sub>8,47</sub></i>	0.2	<i>CTI<sub>3,5</sub></i>	0.2	<i>CTI<sub>83,18</sub></i>	2.685191	<i>CTI<sub>66,63</sub></i>	0.54714
<i>CTI<sub>80,47</sub></i>	0.311377	<i>CTI<sub>25,11</sub></i>	0.279803	<i>CTI<sub>24,15</sub></i>	0.421268	<i>CTI<sub>67,63</sub></i>	0.542556
<i>CTI<sub>54,48</sub></i>	0.347152	<i>CTI<sub>9,11</sub></i>	0.451505	<i>CTI<sub>13,15</sub></i>	0.2	<i>CTI<sub>31,63</sub></i>	0.465819
<i>CTI<sub>52,48</sub></i>	0.350639	<i>CTI<sub>14,12</sub></i>	0.2	<i>CTI<sub>18,16</sub></i>	0.392743	<i>CTI<sub>34,63</sub></i>	0.538951
<i>CTI<sub>50,48</sub></i>	0.2	<i>CTI<sub>46,12</sub></i>	0.2	<i>CTI<sub>43,16</sub></i>	0.2	<i>CTI<sub>61,64</sub></i>	0.2
<i>CTI<sub>54,49</sub></i>	0.2	<i>CTI<sub>41,40</sub></i>	0.2	<i>CTI<sub>83,16</sub></i>	0.382981	<i>CTI<sub>62,60</sub></i>	0.2
<i>CTI<sub>52,49</sub></i>	0.2	<i>CTI<sub>84,40</sub></i>	0.2	<i>CTI<sub>35,37</sub></i>	0.2	<i>CTI<sub>79,60</sub></i>	0.2
<i>CTI<sub>47,49</sub></i>	0.2	<i>CTI<sub>74,39</sub></i>	0.2	<i>CTI<sub>45,37</sub></i>	0.200313	<i>CTI<sub>59,61</sub></i>	0.2
<i>CTI<sub>7,9</sub></i>	0.2	<i>CTI<sub>37,39</sub></i>	0.2	<i>CTI<sub>74,38</sub></i>	0.284815	<i>CTI<sub>79,61</sub></i>	0.378606
<i>CTI<sub>1,9</sub></i>	0.203566	<i>CTI<sub>84,39</sub></i>	0.555264	<i>CTI<sub>40,38</sub></i>	0.2	<i>CTI<sub>63,62</sub></i>	0.2
<i>CTI<sub>12,10</sub></i>	0.369995	<i>CTI<sub>43,71</sub></i>	2.045112	<i>CTI<sub>33,35</sub></i>	0.2	<i>CTI<sub>60,57</sub></i>	0.2
<i>CTI<sub>25,10</sub></i>	0.2	<i>CTI<sub>38,73</sub></i>	2.297199	<i>CTI<sub>38,36</sub></i>	0.2	<i>CTI<sub>77,57</sub></i>	0.286552
<i>CTI<sub>29,50</sub></i>	0.2	<i>CTI<sub>40,73</sub></i>	294.3489	<i>CTI<sub>45,36</sub></i>	0.2	<i>CTI<sub>65,58</sub></i>	0.2
<i>CTI<sub>52,53</sub></i>	0.865944	<i>CTI<sub>76,69</sub></i>	3.379582	<i>CTI<sub>30,31</sub></i>	0.2	<i>CTI<sub>77,59</sub></i>	0.2
<i>CTI<sub>47,53</sub></i>	0.803113	<i>CTI<sub>75,70</sub></i>	3.022053	<i>CTI<sub>27,31</sub></i>	0.2	<i>CTI<sub>58,59</sub></i>	0.2
<i>CTI<sub>50,53</sub></i>	0.658855	<i>CTI<sub>67,70</sub></i>	1.224457	<i>CTI<sub>34,32</sub></i>	0.2	<i>CTI<sub>64,65</sub></i>	0.2
<i>CTI<sub>56,54</sub></i>	0.2	<i>CTI<sub>75,67</sub></i>	0.2	<i>CTI<sub>66,32</sub></i>	0.2	<i>CTI<sub>67,65</sub></i>	0.592518
<i>CTI<sub>53,55</sub></i>	0.2	<i>CTI<sub>69,67</sub></i>	0.2	<i>CTI<sub>67,32</sub></i>	0.2	<i>CTI<sub>31,65</sub></i>	0.519684
<i>CTI<sub>51,56</sub></i>	0.2	<i>CTI<sub>38,46</sub></i>	0.401976	<i>CTI<sub>46,13</sub></i>	0.504952	<i>CTI<sub>34,65</sub></i>	0.592202
<i>CTI<sub>78,56</sub></i>	0.765093	<i>CTI<sub>35,46</sub></i>	0.401015	<i>CTI<sub>11,13</sub></i>	0.455664	<i>CTI<sub>57,66</sub></i>	0.2
<i>CTI<sub>54,51</sub></i>	0.857363	<i>CTI<sub>14,45</sub></i>	0.249702	<i>CTI<sub>16,14</sub></i>	0.2	<i>CTI<sub>66,68</sub></i>	1.217027
<i>CTI<sub>47,51</sub></i>	0.80777	<i>CTI<sub>11,45</sub></i>	0.2	<i>CTI<sub>24,14</sub></i>	0.2	<i>CTI<sub>64,68</sub></i>	0.823188
<i>CTI<sub>50,51</sub></i>	0.662925	<i>CTI<sub>2,3</sub></i>	0.2	<i>CTI<sub>5,22</sub></i>	0.2	<i>CTI<sub>34,68</sub></i>	1.215165
<i>CTI<sub>55,52</sub></i>	0.2	<i>CTI<sub>42,43</sub></i>	0.2	<i>CTI<sub>13,23</sub></i>	0.305892	<i>CTI<sub>31,68</sub></i>	1.141606
<i>CTI<sub>78,52</sub></i>	1.04383	<i>CTI<sub>83,43</sub></i>	1.968492	<i>CTI<sub>16,23</sub></i>	0.530224	<i>CTI<sub>30,28</sub></i>	0.221987
<i>CTI<sub>4,1</sub></i>	0.2	<i>CTI<sub>72,43</sub></i>	0.412337	<i>CTI<sub>31,33</sub></i>	0.2	<i>CTI<sub>32,28</sub></i>	0.2
<i>CTI<sub>7,2</sub></i>	0.651483	<i>CTI<sub>44,41</sub></i>	0.2	<i>CTI<sub>66,33</sub></i>	0.273376		

### **5. Second Proposed Approach:**

The proposed approach considers the idea to negate or, at the very least, minimize the contribution of the DG during a fault, while adding no adverse effects to the network during normal steady state non-fault operation. It introduces the use of fault current limiter (FCL) in series with DG to limit the current of the DG during a fault, and therefore to restore the original relay coordination. The advantage of this solution over others is that it does not require the existing relay protection scheme in a distribution system to be changed adaptively [11]-[12].

Therefore, using this solution, the miscoordination of relays can be solved without the need to change the relay settings or DG disconnecting during fault. The process of determining FCL type whether resistive, inductive or combined and calculating its minimum impedance will be briefly discussed in the following steps:

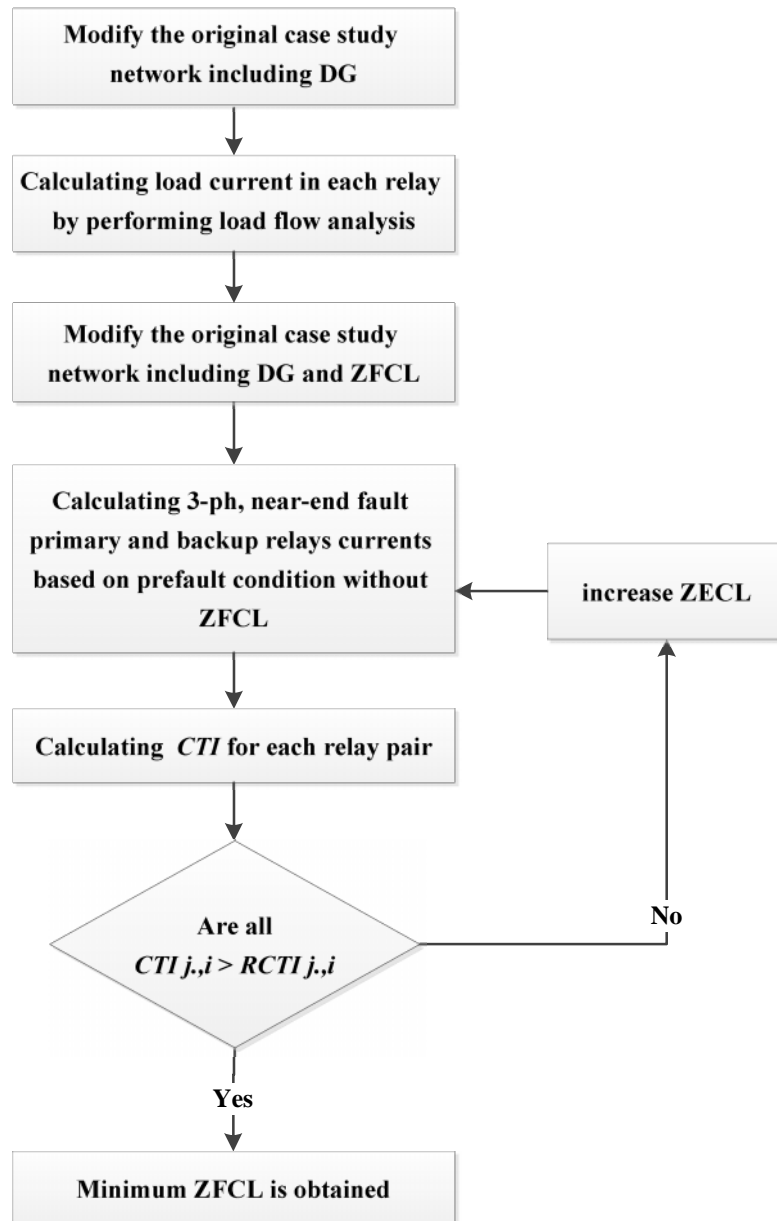
- The first step in this approach is to calculate original relays settings (without DG) as mentioned before in Section 4.B.
- The second step is to start with low value of FCL and then fault calculation is carried out to improve relays coordination.
- Then, the value of FCL is increased step by step and *CTI* of each relay pair is calculated based on fault calculations, taking into account the new value of FCL during fault only and therefore prevent any effect during power flow.
- The above steps are repeated until the lowest value of the *CTI* of miscoordination relay pairs is achieved to a new revised coordination time interval (*RCTI*), Which is near to or lower than the original value of *CTI*.

The steps of the second proposed approach are explained briefly in Fig (3).

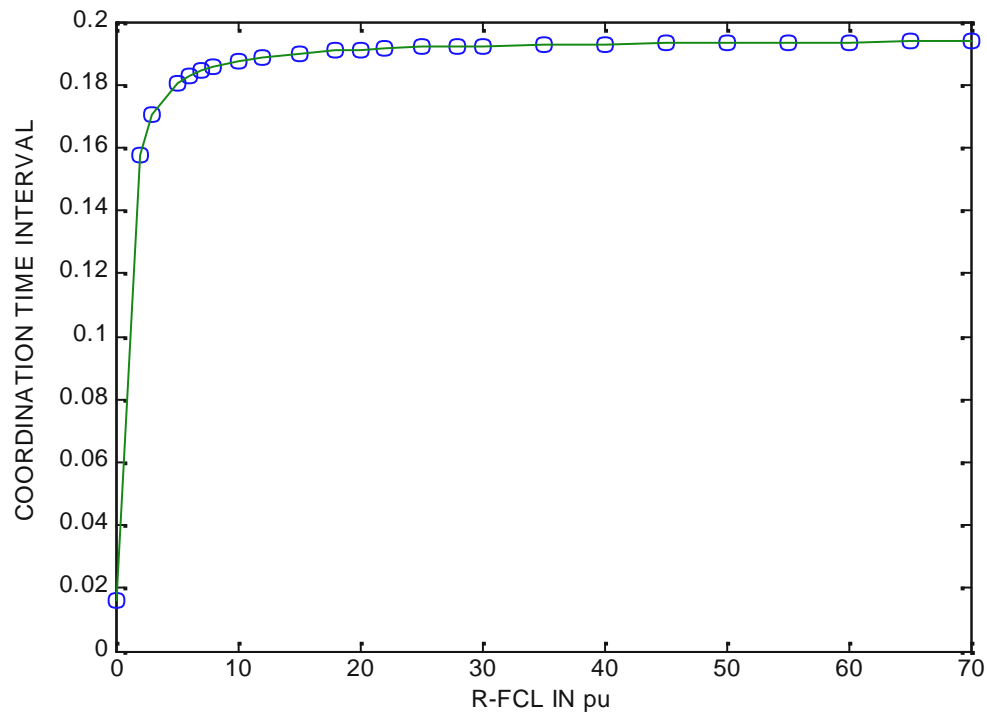
As previously shown in Table (3), the lowest value of *CTI* is occurred for relays pair 49 and 54 which equals to 0.0159 s.

As shown in Table (6), the *CTI* 54,49 is improved nearly to 0.1922 sec (0.96% of the original (*CTI*)) by introducing the resistive FCL of 28 pu or by introducing X-FCL of 35 pu. Finally combined FCL of  $(30+30j)$  pu improves the *CTI* 54,49 to the same value. Therefore, the resistive FCL is considered more effective than the inductive one.

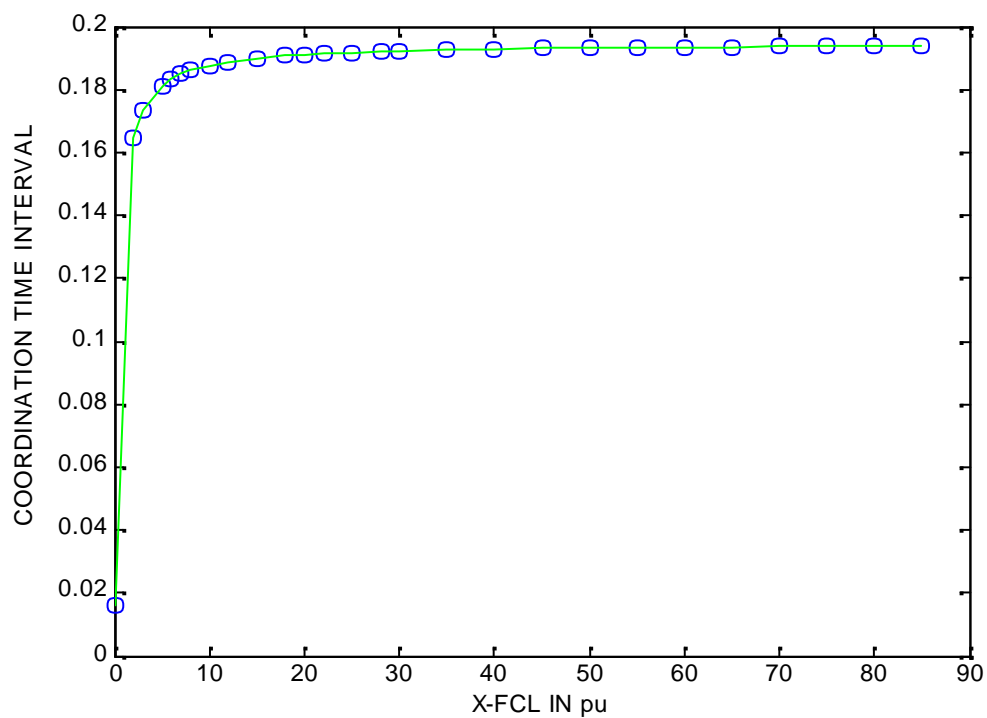
It is obviously shown from Figs (4), (5) and (6) that any increase of FCL above these values has no improvement on *CTI* 54,49.



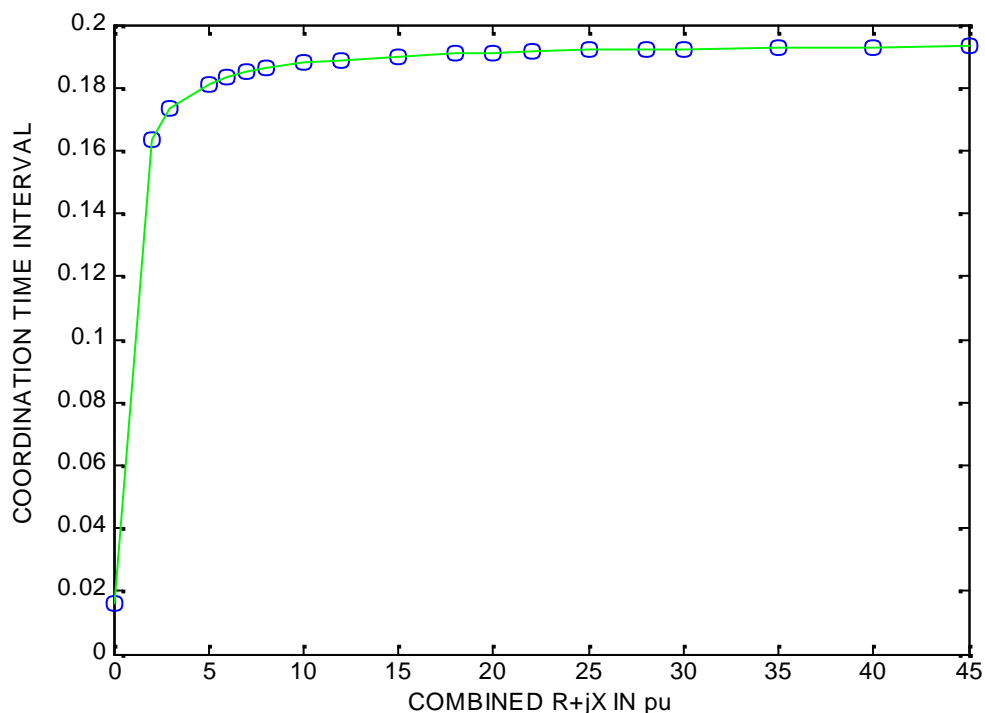
**Figure (3):** Flow chart of the second proposed approach for DOCRs coordination in a power system configuration with DG



**Figure (4):** Coordination time interval CTI 54,49 using R-FCL



**Figure (5):** Coordination time interval CTI 54,49 using X-FCL



**Figure (6):** Coordination time interval CTI 54,49 using Combined Z- FCL

## **6. Conclusion :**

Coordination of DOCRs in presence of DG is introduced using two approaches. The first one is suitable for adaptive relays, relay settings in case of no existing and existing DG have been calculated using (LP) technique based on Matlab optimization toolbox. The second approach is suitable for non adaptive relays, in which, FCL is introduced to restore the coordination of relays without changing of relay settings. The results show that the R-FCL with lower impedance than X-FCL and combined Z-FCL is chosen for the case study. The results given are based on near end, 3- $\phi$  faults at each relay of IEEE-39 bus case study for the two approaches.

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### **Nomenclatures:**

$TDS_i$	Time dial setting of relay $R_i$
$I_{p_i}$	Pick-up current of relay $R_i$
$t_i$	Operating time of the $i$ th primary relay for a near end fault at $i$ (in seconds)
$t_{j,i}$	Operating time of the first back up $j$ th relay for a near end fault at the $i$ th relay
$CTI_{j,i}$	Coordination time interval for backup-primary relay pair ( $j,i$ )