

A NEW COMMON FIXED POINT THEOREM IN INTUITIONISTIC FUZZY METRIC SPACES

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ABSTRACT. In this article, we prove a common fixed point theorem for compatible mapping in intuitionistic fuzzy metric spaces. An example is given to support the main result.

1. INTRODUCTION

Gerald Jungck[5] introduced the concept of compatible mapping which is the generalization of the commuting mapping. Mishra et al.[8] generalized this concept to fuzzy metric spaces. The fuzzy version of the result of Pant[10] was proved by Vasuki. She proved a common fixed point theorem using R-weakly commuting. Common fixed point theorems for weakly commuting maps are given by so many authors[13],[15],[21]. Y.J.Cho introduced the concept of compatible mapping of type (α) [2] and compatible mapping of type (β) [3]. Further some Mathematicians proved common fixed point theorem for compatible mappings in fuzzy metric spaces[18],[17],[19] and intuitionistic fuzzy metric spaces[9],[11],[16],[20],[22]. In this article, we prove a common fixed point theorem for compatible mapping in intuitionistic fuzzy metric spaces.

Definition 1 [14] A binary operation $*$: $[0, 1] \times [0, 1] \rightarrow [0, 1]$ is called a t -norm if the following conditions hold:

- (i) $*$ is associative and commutative;
- (ii) $a * 1 = a, \forall a \in [0, 1]$;
- (iii) $a * b \leq c * d$ whenever $a \leq c$ and $b \leq d, \forall a, b, c, d \in [0, 1]$.

If $*$ is continuous then it is called a continuous t -norm.

Definition 2 [14] A binary operation \diamond : $[0, 1] \times [0, 1] \rightarrow [0, 1]$ is called a t -conorm if the following conditions hold:

- (i) \diamond is associative and commutative;
- (ii) $a \diamond 0 = a, \forall a \in [0, 1]$;
- (iii) $a \diamond b \leq c \diamond d$ whenever $a \leq c$ and $b \leq d, \forall a, b, c, d \in [0, 1]$.

If \diamond is continuous then it is called a continuous t -conorm.

Definition 3 [12] Let X be an arbitrary set, $*$ be a continuous t -norm, \diamond be a

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continuous t -conorm and Let X be an arbitrary set, $*$ be a continuous t -norm, \diamond be a continuous t -conorm and M, N be fuzzy sets on $X^2 \times (0, \infty)$. Consider the following conditions $\forall u, v, w \in X$ and $t > 0$,

- (i) $M(u, v, t) + N(u, v, t) \leq 1$;
- (ii) $M(u, v, 0) = 0$;
- (iii) $M(u, v, t) = 1$ if and only if $u = v$;
- (iv) $M(u, v, t) = M(v, u, t)$;
- (v) $M(u, w, t + s) \geq M(u, v, t) * M(v, w, s)$;
- (vi) $M(u, v, \cdot) : (0, \infty) \rightarrow [0, 1]$ is left continuous;
- (vii) $N(u, v, 0) = 1$;
- (viii) $N(u, v, t) = 0$ if and only if $u = v$;
- (ix) $N(u, v, t) = N(v, u, t)$;
- (x) $N(u, w, t + s) \leq N(u, v, t) \diamond N(v, w, s)$;
- (xi) $N(u, v, \cdot) : (0, \infty) \rightarrow [0, 1]$ is left continuous.

If M satisfies conditions (ii)-(vi), then the pair $(M, *)$ is called fuzzy metric on X . In this case, the triple $(X, M, *)$ is called a fuzzy metric space. If N satisfies conditions (vii)-(xi), then the pair (N, \diamond) is called dual fuzzy metric on X . Then the triple (X, N, \diamond) is called a dual fuzzy metric space.

If $(M, *)$ is a fuzzy metric on X and (N, \diamond) is a dual fuzzy metric on X satisfying condition (i), then the 4-tuple $(M, N, *, \diamond)$ is called an intuitionistic fuzzy metric on X . In this case, the 5-tuple $(X, M, N, *, \diamond)$ is called an intuitionistic fuzzy metric space.

Example 4 [1] Let (X, d) be a metric space. Denote $a * b = ab$ and $a \diamond b = \min\{1, a + b\}$, $\forall a, b \in [0, 1]$ and let M_d and N_d be fuzzy sets on $X \times X \times (0, +\infty)$ defined as follows: $M_d(u, v, t) = \frac{t}{t+d(u,v)}$ and $N_d(u, v, t) = \frac{d(u,v)}{t+d(u,v)}$, $\forall t > 0$, then $(X, M_d, N_d, *, \diamond)$ is an intuitionistic fuzzy metric space.

Definition 5 [6] Let $(X, M, N, *, \diamond)$ be an intuitionistic fuzzy metric space. A sequence $\{u_n\}$ in X is called

- (a) convergent to a point $u \in X$ if and only if $\lim_{n \rightarrow +\infty} M(u_n, u, t) = 1$, and $\lim_{n \rightarrow +\infty} N(u_n, u, t) = 0$, $\forall t > 0$,
- (b) Cauchy if $\lim_{n \rightarrow \infty} M(u_n, u_{n+p}, t) = 1$, and $\lim_{n \rightarrow +\infty} N(u_n, u_{n+p}, t) = 0$, $\forall t > 0$ and $p > 0$.

Definition 6 An intuitionistic fuzzy metric space $(X, M, N, *, \diamond)$ is said to be complete if every Cauchy sequence in X is convergent.

Definition 7 [8] In an intuitionistic fuzzy metric space $(X, M, N, *, \diamond)$, two self mappings A and B are said to be compatible if $\lim_{n \rightarrow \infty} M(ABu_n, BAu_n, t) = 1$ and $\lim_{n \rightarrow \infty} N(ABu_n, BAu_n, t) = 0$ whenever u_n is a sequence in X such that $\lim_{n \rightarrow \infty} Au_n = \lim_{n \rightarrow \infty} Bu_n = w$ for some $w \in X$.

2. MAIN RESULTS

Definition 1 Let Ψ be the class of all non decreasing mappings $\psi : [0, 1] \rightarrow [0, 1]$ and $\eta : [0, 1] \rightarrow [0, 1]$ such that

- (i) $\lim_{n \rightarrow \infty} \psi^n(s) = 1$, $\forall s \in (0, 1]$;
- (ii) $\psi(s) > s$, $\forall s \in (0, 1)$;
- (iii) $\psi(1) = 1$;
- (iv) $\lim_{n \rightarrow \infty} \eta^n(r) = 0$, $\forall r \in [0, 1)$;
- (v) $\eta(r) < r$, $\forall r \in (0, 1)$;
- (vi) $\eta(0) = 0$.

Example 2 Define $\psi : [0, 1] \rightarrow [0, 1]$ by $\psi(s) = \frac{2s}{s+1}, \forall s \in [0, 1]$.

$$\psi^2(s) = \frac{4s}{3s+1}, \psi^3(s) = \frac{8s}{7s+1}, \dots, \psi^n(s) = \frac{2^n s}{(2^n - 1)s + 1}, \forall s \in [0, 1].$$

$$\lim_{n \rightarrow \infty} \psi^n(s) = \lim_{n \rightarrow \infty} \frac{2^n s}{(2^n - 1)s + 1} = 1, \forall s \in (0, 1).$$

Clearly, $\psi(s) > s, \forall s \in (0, 1)$ and $\psi(1) = 1$.

Define $\eta : [0, 1] \rightarrow [0, 1]$ by $\eta(r) = \frac{r}{2-r} \forall r \in [0, 1]$.

$$\eta^2(r) = \frac{r}{4-3r}, \eta^3(r) = \frac{r}{8-7r}, \dots, \eta^n(r) = \frac{r}{2^n(1-r)+r}, \forall r \in [0, 1].$$

$$\lim_{n \rightarrow \infty} \eta^n(r) = \lim_{n \rightarrow \infty} \frac{r}{2^n(1-r)+r} = 0, \forall r \in [0, 1).$$

Clearly, $\eta(r) < r, \forall r \in (0, 1)$ and $\eta(0) = 0$.

Proposition 3 Let A and B be compatible mappings of an intuitionistic fuzzy metric space $(X, M, N, *, \diamond)$ into itself. If $Aw = Bw$ for some $w \in X$, then $ABw = BA w$.

Proof. Suppose that $\{u_n\}$ is a sequence in X defined by $u_n = w, n = 1, 2, \dots$ for some $w \in X$ and $Aw = Bw$. Then we have $Au_n, Bu_n \rightarrow Aw$ as $n \rightarrow \infty$. Since A and B are compatible mapping,

$$M(ABw, BA w, t) = \lim_{n \rightarrow \infty} M(ABu_n, BA u_n, t) = 1,$$

$$N(ABw, BA w, t) = \lim_{n \rightarrow \infty} N(ABu_n, BA u_n, t) = 0.$$

Hence, we have $ABw = BA w$.

Proposition 4 If A and B are compatible maps on an intuitionistic fuzzy metric space X and $Au_n, Bu_n \rightarrow w$ for some $w \in X, (u_n$ being a sequence in $X)$ then $ABu_n \rightarrow Bw$ provided B is continuous (at w).

Proof. Since B is continuous at $w, BA u_n \rightarrow Bw$ and $BBu_n \rightarrow Bw$. Since A and B are compatible maps, $M(ABu_n, BA u_n, t) \rightarrow 1$ and $N(ABu_n, BA u_n, t) \rightarrow 0$ as $n \rightarrow \infty$.

$$M(Bw, ABu_n, t) \geq M(Bw, BA u_n, \frac{t}{2}) * M(BA u_n, ABu_n, \frac{t}{2}),$$

$$N(Bw, ABu_n, t) \leq N(Bw, BA u_n, \frac{t}{2}) \diamond N(BA u_n, ABu_n, \frac{t}{2}).$$

Taking limit as $n \rightarrow \infty$, we get

$$\lim_{n \rightarrow \infty} M(Bw, ABu_n, t) = 1 \text{ and } \lim_{n \rightarrow \infty} N(Bw, ABu_n, t) = 0.$$

Hence, $ABu_n \rightarrow Bw$.

Theorem 5 Let A and B be self maps on a complete intuitionistic fuzzy metric space X and $\psi \in \Psi$ such that satisfy the following conditions:

(I) $A(X) \subset B(X)$,

(II) $M(A(u), A(v), t) \geq \psi(M(Bu, Bv, t))$ and $N(A(u), A(v), t) \leq \eta(N(Bu, Bv, t)) \forall u, v \in X$ and $t > 0$,

(III) A or B is continuous.

Assume that A and B are weakly compatible. Then A and B have a unique common fixed point in X .

Proof. Let $u_0 \in X$ and $A(X) \subset B(X)$ define a sequence u_n in $X, \forall n \in N$ as follows:

$$Au_n = B(u_{n+1})$$

Then for all $t > 0$,

$$\begin{aligned} M(Au_n, Au_{n+1}, t) &\geq \psi(M(Bu_n, Bu_{n+1}, t)) \\ &= \psi(M(Au_{n-1}, Au_n, t)) \\ &\geq \psi^2(M(Bu_{n-1}, Bu_n, t)) \\ &\dots \\ &\geq \psi^n(M(Au_0, Au_1, t)). \end{aligned}$$

That is, $M(Au_n, Au_{n+1}, t) \geq \psi^n(M(Au_0, Au_1, t))$.

$$\begin{aligned} N(Au_n, Au_{n+1}, t) &\leq \eta(N(Bu_n, Bu_{n+1}, t)) \\ &= \eta(N(Au_{n-1}, Au_n, t)) \\ &\leq \eta^2(N(Bu_{n-1}, Bu_n, t)) \\ &\dots \\ &\leq \eta^n(N(Au_0, Au_1, t)). \end{aligned}$$

That is, $N(Au_n, Au_{n+1}, t) \leq \eta^n(N(Au_0, Au_1, t))$.

By taking limit as $n \rightarrow \infty$, and since $\lim_{n \rightarrow \infty} \psi^n(s) = 1, \forall s \in (0, 1]$ and $\lim_{n \rightarrow \infty} \eta^n(r) = 0, \forall r \in [0, 1)$, $\lim_{n \rightarrow \infty} M(Au_n, Au_{n+1}, t) = 1$ and $\lim_{n \rightarrow \infty} N(Au_n, Au_{n+1}, t) = 0$.

Now for any positive integer p ,

$$\begin{aligned} M(Au_n, Au_{n+p}, t) &\geq M(Au_n, Au_{n+1}, \frac{t}{p}) * \dots * M(Au_{n+p-1}, Au_{n+p}, \frac{t}{p}). \\ N(Au_n, Au_{n+p}, t) &\leq N(Au_n, Au_{n+1}, \frac{t}{p}) \diamond \dots \diamond N(Au_{n+p-1}, Au_{n+p}, \frac{t}{p}). \end{aligned}$$

Taking limit $n \rightarrow \infty$, we have,

$$\begin{aligned} \lim_{n \rightarrow \infty} M(Au_n, Au_{n+p}, t) &\geq \lim_{n \rightarrow \infty} M(Au_n, Au_{n+1}, \frac{t}{p}) * \dots * \lim_{n \rightarrow \infty} M(Au_{n+p-1}, Au_{n+p}, \frac{t}{p}) \\ &\geq 1 * \dots * 1 \\ &= 1. \end{aligned}$$

That is,

$$\lim_{n \rightarrow \infty} M(Au_n, Au_{n+p}, t) = 1.$$

$$\begin{aligned} \lim_{n \rightarrow \infty} N(Au_n, Au_{n+p}, t) &\leq \lim_{n \rightarrow \infty} N(Au_n, Au_{n+1}, \frac{t}{p}) \diamond \dots \diamond \lim_{n \rightarrow \infty} N(Au_{n+p-1}, Au_{n+p}, \frac{t}{p}) \\ &\leq 0 \diamond \dots \diamond 0 \\ &= 0. \end{aligned}$$

That is,

$$\lim_{n \rightarrow \infty} N(Au_n, Au_{n+p}, t) = 0.$$

Hence, $\{Au_n\}$ is a Cauchy sequence in X .

Since $(X, M, N, *, \diamond)$ is a complete intuitionistic fuzzy metric space, there exists $w \in X$ such that $\lim_{n \rightarrow \infty} M(Au_n, w, t) = 1, \lim_{n \rightarrow \infty} M(Bu_n, w, t) = 1$ and $\lim_{n \rightarrow \infty} N(Au_n, w, t) = 0, \lim_{n \rightarrow \infty} N(Bu_n, w, t) = 0$ for each $t > 0$.

Suppose A is continuous. Since A and B are compatible and A is continuous, by Proposition 4, $BAu_n \rightarrow Aw$.

Now,

$$M(Au_n, AAu_n, t) \geq \psi(M(Bu_n, BAu_n, t)),$$

$$N(Au_n, AAu_n, t) \leq \eta(N(Bu_n, BAu_n, t)).$$

Taking limit as $n \rightarrow \infty$, we get

$$M(w, Aw, t) \geq \psi(M(w, Aw, t)) \geq M(w, Aw, t),$$

$$M(w, Aw, t) \leq \eta(N(w, Aw, t)) \leq N(w, Aw, t).$$

This is possible only when $M(w, Aw, t) = 1$ and $N(w, Aw, t) = 0$. That is $Aw = w$. Since $A(X) \subset B(X)$, there exists w_1 in X such that $w = Aw = Bw_1$. Now,

$$M(AAu_n, Aw_1, t) \geq \psi(M(BAu_n, Bw_1, t)),$$

$$N(AAu_n, Aw_1, t) \leq \eta(N(BAu_n, Bw_1, t)).$$

Taking limit as $n \rightarrow \infty$, we get

$$M(Aw, Aw_1, t) \geq \psi(M(Aw, Bw_1, t)) = \psi(1) = 1,$$

$$N(Aw, Aw_1, t) \leq \eta(N(Aw, Bw_1, t)) = \eta(0) = 0.$$

That is $Aw_1 = Bw_1$.

Now, we have $Aw = Aw_1$. By Proposition 3, $ABw_1 = BAw_1$.

$$M(Aw, Bw, t) = M(ABw_1, BAw_1, t) = 1,$$

$$N(Aw, Bw, t) = N(ABw_1, BAw_1, t) = 0.$$

Hence, $Aw = Bw = w$. Hence A and B have a common fixed point in X . **Uniqueness:**

Assume $\bar{w} \neq w$ for some $\bar{w} \in X$, is another common fixed point in X . Then for $t > 0$, we have,

$$\begin{aligned} M(w, \bar{w}, t) &= M(A(w), A(\bar{w}), t) \\ &\geq \psi(M(B(w), B(\bar{w}), t)) \\ &\dots \\ &\geq \psi^n(M(B(w), B(\bar{w}), t)), \end{aligned}$$

$$\begin{aligned} N(w, \bar{w}, t) &= N(A(w), A(\bar{w}), t) \\ &\leq \eta(N(B(w), B(\bar{w}), t)) \\ &\dots \\ &\leq \eta^n(N(B(w), B(\bar{w}), t)). \end{aligned}$$

Taking limit as $n \rightarrow \infty$ and by our assumption,

$$M(u, v, t) \geq \lim_{n \rightarrow \infty} \psi^n(M(u, v, t)) = 1,$$

$$N(u, v, t) \leq \lim_{n \rightarrow \infty} \eta^n(N(u, v, t)) = 0.$$

That is, $M(u, v, t) = 1$ and $N(u, v, t) = 0$.

Therefore, $u = v$.

Hence T has a unique fixed point in X .

Example 6 Let $X = [0, \infty)$ with the metric d defined by $d(u, v) = |u - v|$, define $M(u, v, t) = \frac{t}{t+d(u,v)}$, and $N(u, v, t) = \frac{d(u,v)}{t+d(u,v)} \forall u, v \in X$ and $t > 0$. Note that, $(X, M, N, *, \diamond)$ where $a * b = ab$ and $a \diamond b = \min\{1, a + b\}$ is a complete intuitionistic fuzzy metric space.

The maps $A, B : X \rightarrow X$ is defined by $A(u) = \frac{2+u}{3}$ and $B(u) = u$. Let $u_n = 1 - \frac{1}{n}$

$$\begin{aligned} \lim_{n \rightarrow \infty} M(ABu_n, BAu_n, t) &= \lim_{n \rightarrow \infty} M(Au_n, B\frac{2+u_n}{3}, t) \\ &= \lim_{n \rightarrow \infty} M(\frac{2+u_n}{3}, \frac{2+u_n}{3}, t) \\ &= 1. \end{aligned}$$

$$\begin{aligned} \lim_{n \rightarrow \infty} N(ABu_n, BAu_n, t) &= \lim_{n \rightarrow \infty} N(Au_n, B\frac{2+u_n}{3}, t) \\ &= \lim_{n \rightarrow \infty} N(\frac{2+u_n}{3}, \frac{2+u_n}{3}, t) \\ &= 0. \end{aligned}$$

$\lim_{n \rightarrow \infty} M(ABu_n, BAu_n, t) = 1$ and $\lim_{n \rightarrow \infty} N(ABu_n, BAu_n, t) = 0$.

$\lim_{n \rightarrow \infty} Au_n = \lim_{n \rightarrow \infty} \frac{2+u_n}{3} = \lim_{n \rightarrow \infty} \frac{2+(1-\frac{1}{n})}{3} = 1$.

$\lim_{n \rightarrow \infty} Bu_n = \lim_{n \rightarrow \infty} u_n = \lim_{n \rightarrow \infty} 1 - \frac{1}{n} = 1$.

Therefore, A and B are compatible mapping. Also $AX \subset BX$ and B is continuous.

Define the map $\psi : [0, 1] \rightarrow [0, 1]$ by $\psi(s) = \frac{2s}{s+1}$ for each $s \in [0, 1]$ and $\psi \in \Psi$.

$$M(A(u), A(v), t) \geq \psi(M(B(u), B(v), t))$$

$$\text{if } M(\frac{2+u}{3}, \frac{2+v}{3}, t) \geq \psi(M(u, v, t))$$

$$\text{That is if } \frac{t}{t + d(\frac{2+u}{3}, \frac{2+v}{3})} \geq \frac{\frac{2t}{t+d(u,v)}}{\frac{t}{t+d(u,v)} + 1}$$

$$\text{That is if } \frac{t}{t + |\frac{2+u}{3} - \frac{2+v}{3}|} \geq \frac{\frac{2t}{t+|u-v|}}{\frac{t}{t+|u-v|} + 1}$$

$$\text{That is if } \frac{t}{t + \frac{|u-v|}{3}} \geq \frac{t}{t + \frac{|u-v|}{2}}$$

$$\text{That is if } t + \frac{|u-v|}{2} \geq t + \frac{|u-v|}{3}$$

$$\text{That is if } 3 \geq 2.$$

Define the map $\eta : [0, 1] \rightarrow [0, 1]$ by $\eta(r) = \frac{r}{2-r}$ for each $r \in [0, 1]$ and $\eta \in \Psi$.

$$N(A(u), A(v), t) \leq \eta(N(B(u), B(v), t))$$

$$\text{if } N\left(\frac{2+u}{3}, \frac{2+u}{3}, t\right) \leq \frac{N(u, v, t)}{2 - N(u, v, t)}$$

$$\text{That is if } \frac{d\left(\frac{2+u}{3}, \frac{2+u}{3}\right)}{t + d\left(\frac{2+u}{3}, \frac{2+u}{3}\right)} \leq \frac{\frac{d(u, v)}{t+d(u, v)}}{2 - \frac{d(u, v)}{t+d(u, v)}}$$

$$\text{That is if } \frac{\left|\frac{2+u}{3} - \frac{2+v}{3}\right|}{t + \left|\frac{2+u}{3} - \frac{2+v}{3}\right|} \leq \frac{\frac{|u-v|}{t+|u-v|}}{2 - \frac{|u-v|}{t+|u-v|}}$$

$$\text{That is if } \frac{\frac{|u-v|}{3}}{t + \frac{|u-v|}{3}} \leq \frac{|u-v|}{2t + |u-v|}$$

$$\text{That is if } 2t + |u-v| \leq 3t + |u-v|$$

$$\text{That is if } 2 \leq 3.$$

All the conditions of the previous theorem are verified.

Then 1 is the unique fixed point.

Hence A and B have the unique common fixed point in X .

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