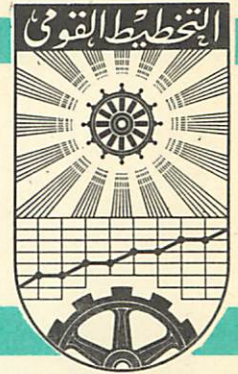


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An Introduction To The
Input-Output Model

By

Dr. G. Eleish

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National Planning Committee, Cairo

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Historical background

Consistent thinking is no doubt "a moral obligation"⁽¹⁾ and if it is so for intelligent human beings it is certainly much more so for rational economists. But even a rational well disciplined economist is often at a loss when confronted with the highly complicated mechanisms which govern and rule economic decisions. This feeling of uncertainty is even more vivid when he is faced with the unsurmountable difficulties which he has to overcome when dealing with the so-called underdeveloped economies. These difficulties are further enhanced by such limitations, as the lack of statistics, which the latter economies put upon the tools with which he is acquainted and hopes to discover the "invisible hand" which turns the economic wheel in the more advanced economies. In such case, the ideal state of consistent thinking, although remains a desired goal, could not be lived up to all the time. But the rational economist, nevertheless, is in constant search for the proper analytical tool which keeps him within the vicinity of that thinking.

In fact the awareness of the economist of the considerable specialization within each sector of the economy and among the different economies, besides leading to the formulation of such elaborate theories as the comparative cost theory, made him always timid to explore the mysterious sphere of economic interdependency. Furthermore it led him to adopt a certain analytical tool, one which came to be known as partial analysis. This partial analysis was a predominate feature of economic analysis up until a very short time ago. This is despite the equal awareness of the fact that the different sectors of the economy, whatever their degree of specialization may be, could not work in complete isolation from the other sectors of the economy. This awareness is clearly illustrated by the example of the "production of a pin" which Adam Smith forwarded to illustrate the extreme specialization within the economy.

(1) This term is borrowed from a delightful memorandum written by Prof. Ragnar Frisch and published by the National Committee, Cairo. June 19, 1960.

Partial analysis, however, is an indispensable tool in economic understanding particularly if we desire to enhance our knowledge about the operation of the market economy. Marshall's partial equilibrium system in fact could be looked upon as a simplification of the equilibrium theory. However, it does not claim to be looking at the economy as an entity; but rather it traces the changes within individual sectors assuming, of course, that other things will remain unchanged. The changes in the behavior of the consumers and the producers of a particular commodity are examined, with prices and outputs of that commodity being the crucial points. This type of relationship is presented in a set of supply and demand functions, with changes in the level of income or of outputs of the consuming sector appearing as shifts in the demand functions. Similar shifts in the supply functions of the using sector may appear with changes in other uses of its inputs.⁽¹⁾ In fact, what the partial analyst would generally do is to isolate the effects of certain variables and attempts to detect the results of their interaction while assuming the other variables in the economy to be constant. While this approach is commendable in the sphere of physical sciences it is less meaningful in economics as the other variables rarely stay without changing. This is due, of course, to the complicated nature of the economic mechanism and the fact that there exists a great deal of interdependence among the different economic sectors.

The idea of interdependence in the economy, as we have mentioned before, was recognized by Adam Smith, and even by earlier economists.⁽²⁾ The "Tableau Economique" in which François Quesnay⁽³⁾ attempted to demonstrate the flow of wealth through the economy is but a definite recognition of that idea. In fact interindustry models are generally traced back to those "tableaux". However, it is generally maintained⁽⁴⁾ that the present development in the field of interindustry economics is largely indebted to the inspiration provided by the work of "Leon Walras" who developed a complex and abstract model which made that phenomenon its main theme. He recognized the fact that "everything in the economy is dependent upon everything else" and his model was built with the aim of examining the requisites for general equilibrium. It contained a number of equations which described the cost structure in the production sectors, the consumers incomes and expenditures as well as the total supply and demand of the different commodities and primary inputs. He took into consideration the substitutability of one product by the other as well assuming that industries would compete for the factors of production, two points to be dropped

(1) Chenery and Clark, "Interindustry Economics", p. 2.

(2) As early as 1759, a draft of what later developed into Wealth of Nations existed in Smith's notes but it was not until March 9, 1776, did the work come from the press. See Robert B. Downs, "Books that Changed the World," p. 42.

(3) François Quesnay published his tables in 1758.

(4) Chenery and Clark, "Interindustry Economics", p. 2.

later, as we shall see, by Prof. Leontief. The Walrasian system: was criticised later as being "an example of the emptiness of economic theory at this level of abstraction, since few interesting conclusions about economic reality can be drawn from the formal properties of the model, and the system as formulated does not lend itself to empirical verification." (1)

Other economists who contributed in this field are Pareto and Cassel who aimed at perfecting the model of Walras. However, it was always felt that their models had to be simplified in order that their functional relations could be statistically determined. At this point one should not underestimate the contribution made by Prof. Ragner Frisch of Norway in his paper "Circulation Planning" which appeared in *Econometrica* in 1934 in which he discussed the case of a closed economic system as well as that of an open one, both with determinants which were equal to 0. (2) In that article he put forward a set of equations which resembled in essence those of the Input-Out Model. (3)

However, it was Prof. Wassily Leontief who thought of these ideas not merely as theoretical sophistications but as an inspiration for his great empirical work. (4) Unlike Prof. Frisch he discussed the case of an open system with non-vanishing determinant. Furthermore he was the first to attempt an empirical application of the general equilibrium theory. Although his work on an empirical model for the American economy started in 1931, his first results were published in 1936. (5) It was Prof. Leontief who simplified the Walrasian model to the extent at which it could be statistically determined. As we mentioned before, he dispensed with the limitations Walras put upon the factor supplies as well as that of substitution among inputs. In doing that he accepted the original assumption of Walras of fixed "coefficients of production." The Leontief model eliminates the effects of prices on the composition of consumer demand, and the demand for intermediate goods as well as that for the factors of production and in doing that it "precludes many of the adjustments characterizing the Walrasian Concept of general Equilibrium." (6)

(1) Ibid, p. 3.

(2) Ragner Frisch, "Some Basic Notions of Input-Output Analysis", National Planning Committee, Cairo, 1957, p. 8.

(3) Ibid, p.7.

(4) W. Duane Evans and Marvin Houffenberg, "The Interindustry Relations study for 1947 U.S. Department of Labour Statistics."

(5) Leontief's basic ideas were published in his article "Quantitative Input-Output Relations in the Economic System of the United States, The Review of Economics and Statistics" Vol. 18, August 1936.

(6) Chenery and Clark, "Interindustry Economics", p. 3.

As it could be observed the approach of a Leontief analyst would be in sharp contrast to that of a partial analyst. While the latter studies the effects of changes in certain magnitudes and attaches no importance to the effects of these changes on the rest of the economy, the Leontief analyst considers the study of these changes his prime object. He takes on the other hand the equilibrium adjustment of input properties as given and does not attach great importance to the assumption of maximizing behavior.(1) Moreover he does not think of the changes in the supply and demand of the different commodities as a result in the changes in prices but rather due to changes in the demand function of the different sectors which are the result of changes in the levels of production. In the short run, the Leontief analyst would think of the changes in demands as having direct influence on output rather than on prices.

The aggregative income analyst, however, has much more in common with the Leontief Analyst. Uniform aggregate behaviors which generally could be determined statistically are corner stones in their analysis. While this is so the partial analyst attempts to rationalize, on the basis of theoretical justifications, the changes involving certain isolated magnitudes. They both (i.e. the former) make assumptions about the autonomous elements in their systems and try to reach the effects of changes in these elements on the level of production or income through a set of coefficients indicating the structure of the economy in the case of the Leontief model or through a set of propensities indicating the response of the rest of the economy to these changes in the case of the aggregate income approach.

However, it must be remembered that a major point of difference still exists between the two analysts and that is the extreme importance which the Leontief analyst attaches to the interdependence in the economy, a point which the aggregative income analyst takes only into consideration but does not exert any effort to bring it into the forefront.

Since the publication of the input-output tables for the American economy for the years 1919 and 1929, remarkable progress had been made, both in techniques of constructing and utilizing the tables. For a while, the field of Input-Analysis was limited to a number of specialized economists. Although, still largely so the technique has become an obligatory course in economics and many economists are eager to learn more about it. Governments in different parts of the world have become aware of the usefulness of that technique in designing their economic policy and we find that an increasing number of them have constructed tables for their economies or are in the process of doing so. This, of course, is one of the remarkable results of the Leontief contribution to economic theory.

Recent developments in economics and statistics, however, provided us with alternative models. Linear programming techniques, although overcome the assumption of fixed input coefficients,(2) have so far

(1) Ibid p. 4.

(2) Chenery and Clark, p. 3.

been applied to the case of single plants. Nevertheless it presents a lineal continuation of thinking and offers other choices in the field of interindustry models.

As we will see later the input-output model has been criticised on several grounds. Some of these are valid and others have no firm ground upon which to stand. The most common among the latter type is the attempt on behalf of some economists to be little Leontief's great contribution on the account that it was, after all, an old Walrasian idea; but as someone said "everything of importance has been said before by someone who did not discover it."

Economic models, a positive step for consistent thinking

Economic models have become an essential tool in economic analysis. In fact, the latter depends a great deal on how the available data are set in such models. Although the economic analyst is limited in forming such models by the restricted availability of the required data more than by his ability to form them, at least theoretically, yet it is the formation of such models that lead to the discovery of the inconsistencies in the available data as well as the gaps in them. It has also become a recognized fact that in order to carry out a certain economic analysis one has to investigate and describe in a comprehensive manner the features of the economy which are of relevance to that type of analysis. These features are often expressed in terms of magnitudes of certain variables which among themselves describe the prevailing structure of the economy. However, in doing that certain definitional relations have to be satisfied. For instance the gross production from sector i could be expressed as an equal sum of the demand on the production of that sector for intermediate consumption plus the demand for final use. This definitional relation could be represented by the following simple equation:

$$X_i = N + Y$$

where N is the demand for intermediate consumption and Y is the demand for final use. But this is only one sector and only one relation. The economy, however, has other sectors and other magnitudes and all are governed by other definitional relations. To be consistent, one must make sure that these relations are fulfilled and not only one of them. If several macroeconomic magnitudes are estimated or planned independently such a requirement would necessitate considerable attention and care that it is safe to state that without the aid of a comprehensive economic model it would be next to impossible to reach any consistent conclusions.

But the definitional relations are not the only relations which should be fulfilled. An economy, at any point of time, has a certain underlying structure and any consistent analytical approach should take this structure into consideration. It would be absurd to think of a future development program which is incompatible with the prevailing structure of an economy. However, this does not mean that

one should think of a certain structure in a static sense but only to indicate that any deliberate change in that structure should be compatible with the underlying one. In any case there is always a set of structural relations which exist in the economy, the interrelations amongst which are highly complicated, a fact which makes the reliance on an economic model an indispensable tool if we ever attempt to examine intimately the structure of the economy.

To illustrate the structural relations let us assume, on the other hand, that in order to produce one unit from sector j we need to have certain deliveries from other sectors plus a certain delivery from imports and other deliveries from primary factors like labor and profits on capital. This could be expressed as follows: $X_j = \sum_i X_{ij} + M_j + V_j$ ($i = 1, 2, \dots, n$) (2) where X_{ij} indicates the delivery from sector i to sector j and M_j indicates the inputs from imports into sector j and V_j indicates the inputs of primary factors or the value added in sector j .

In the meantime these deliveries could be related to the production of sector j through a set of coefficients which indicate the proportion of each input needed for the production of one unit from sector j . This is assuming that there is a linear relation between the production of the sector and the inputs needed for that production. In other words we assume that the proportion of the inputs will not vary by a change in the size of production. These relations could be expressed as follows:

$$X_j = \sum_i a_{ij} X_j + m_j X_j + V_j X_j \quad (i = 1, 2, \dots, n) \quad (3)$$

where a_{ij} indicates the proportion of the input from sector i which is necessary for the production of one unit from sector j and m_j indicates the proportion of inputs from imports which are needed for the production of one unit from sector j , and V_j indicates the proportion of primary inputs or value added created by a production of one unit from sector j .

This is only a simple illustration of a structural relation which describes the structure of only one sector of the economy. But there are many other sectors and there are as many relations of this type as there are sectors. Also there are many other types of structural relations and any future development could not be conceived independently of the prevailing structure of the economy.

By now it has become clear that unless we systematize the economic concepts, whether these are definitional or structural, in a comprehensive model we may never be able to reach constructive conclusions regarding economic problems which we have to deal with and even if we reach any such conclusions we will not possess a tool for testing their logical consistency. Of course an economic model should not be conceived as a magic tool capable of answering all our questions and delivering answers with complete accuracy. Such models generally contain assumptions and reduce the complicated economic relation into simplified formulas and seek reasonable approximation of results.

In fact this very nature of the economic models makes the question of what sort of specifications are relevant and necessary and what simplifications are permissible in the model we intend to use for a particular problem, a prominent one indeed. There is not one economic model to solve every economic problem, but rather for every problem a suitable model to deal with it. In this article we are only dealing with one particular model, i.e. the Input-Output model.

The underlying concepts of the input-output model

The Input-Output Model and its utilization has been extensively discussed by many writers and the literature on that subject is increasing rapidly.(1) However, as these articles intend to put before the reader, who may be entrusted by such work, the experience of the writer in the field of construction and utilization of the Input-Output model in a developing economy, we find it necessary to refer, in as simplified way as possible, to the basic concepts of that method as well as the mathematical aspects (2) involved in its utilization. We will be dealing mainly with the simplest input-output model or that which is referred to as the "open Leontief model." It is called an "open system" because it treats certain sectors of the economy as exogenous sectors. In other words the magnitudes of those sectors are generally considered as given and not derived from a solution of the model. As the stock of capital needed for the creation of certain productive capacities is included in that exogenous part of this system, it is therefore considered a static model because we will be unable to reach a solution which tells us the amount of capital requirements which satisfies our particular target. These points., however, may be discussed in some details later but reference to them was made only to indicate that there are other complicated forms of the input-output model. Nevertheless it is safe to state that these forms could be treated as generalizations of this simple model.

As we have mentioned before, the input-output method is another form of general equilibrium analysis. It is based on the cost structure of the different types of production and like all the other economic models it rests upon certain assumptions about economic behavior and observes certain definitional relations among its variables. But unlike many others, the input-output model is a multi-sector model and aims mainly at illustrating the interdependency among the different sectors of the economy. One can hardly conceive of any change in the demand for the production of one sector without this change having a chain of direct as well as indirect reactions on the other sectors of the economy. Let us assume for instance that with an anticipated increase in per-capita income we were able to project, through utilization of such tools as income elasticity of demand, certain increase in the demand for industrial commodities. Let us also assume that all industries could be grouped into one sector and that we know the inputs needed for the production of that sector. Table 1 makes it clear that in order to produce industrial goods, the industry sector would require inputs from the other sectors. It will have to buy agricultural products, energy, industrial products

(1) See "Input-Output Bibliography", by Charlotte E. Taskier of the Harvard Economic Research Project, a United Nations Publication.

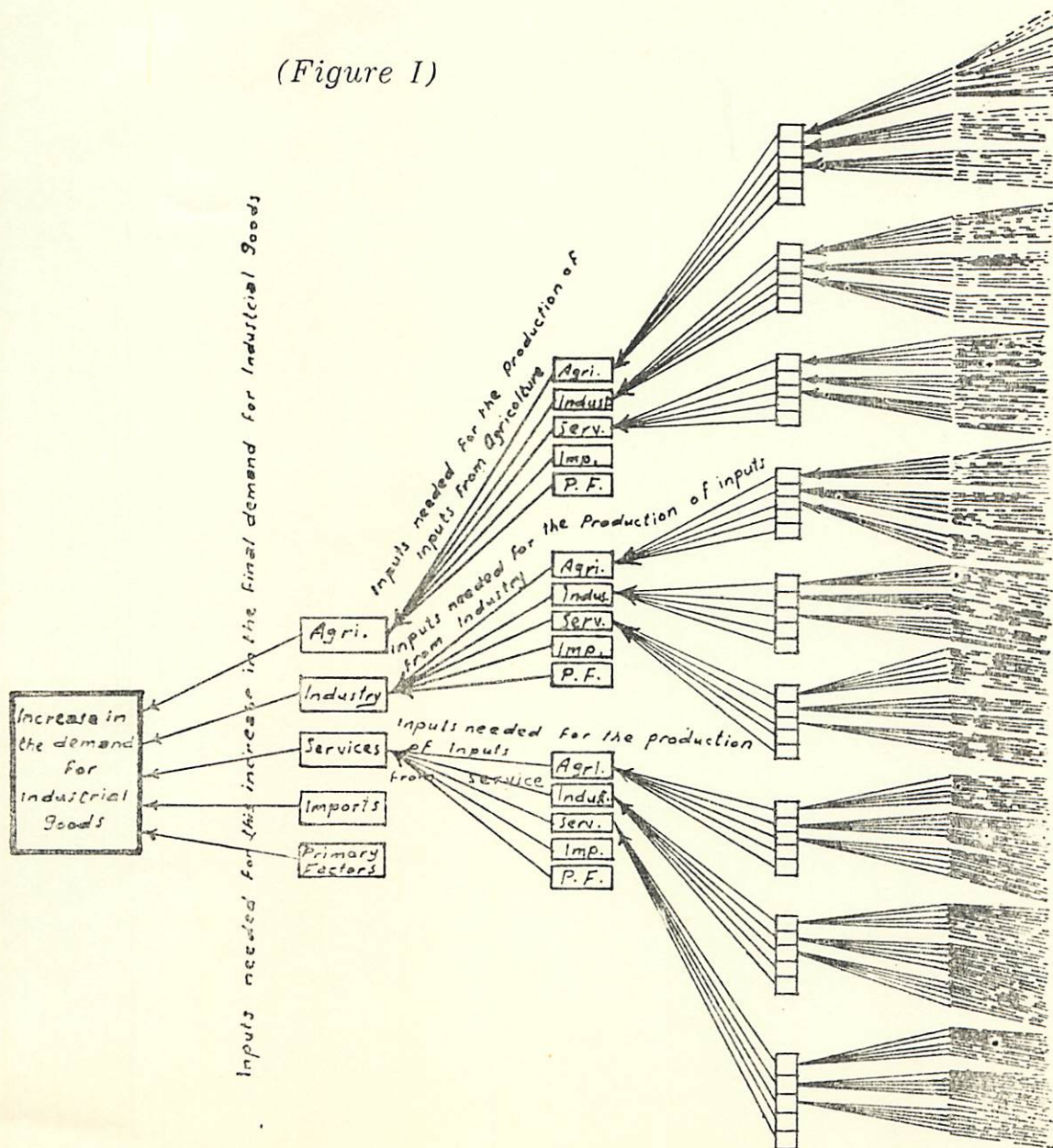
(2) This will be discussed in future articles.

from itself, transportation facilities, construction activities, and services and some imported goods as well as primary inputs. These purchases represent the direct input requirements for the production of the sector industry. But this is not the whole story as these purchases represent in themselves increases in the demand for commodities from the sectors concerned. And those increases in demand mean increases in production and in its turn the increase in the production of every sector requires a variety of inputs of raw materials, intermediate goods and imports. In fact, the very essence of interdependency among the different sectors of the economy is responsible for the creation of a series of reactions which are generally extended to an ever increasing number of sectors. Although the impact of these reactions become progressively weaker (1) yet their total is significantly large to be ignored. The complicated nature of these direct and indirect reactions could be easily conceived in the attached illustration. (Figure 1)

However, it must be remembered that this complicated mechanism which the above illustration made crystal clear, is only the product of an increase in the demand for the production of one sector. Now it is left to the imagination of the reader to consider the case where the demand for other commodities increase simultaneously as they generally do in practice. Here we are faced with the dilemma of quantifying these reactions and as one can see it is beyond any human mind to trace such reactions except through a systematic tool of analysis. In fact, this is the greatest asset of the input-output table. It could tell us, through a set of coefficients, which are generally referred to as "the coefficients of direct and indirect requirements", the total requirements from each sector to satisfy a certain increase in the demand for some commodities. This, being the case, the input-output table, could provide us with answers to a variety of questions which are of great importance particularly in the field of national planning. For instance what would be the effect of a particular investment program in road construction or irrigation. These effects could be translated as total input requirements from both domestic production and imports, labor requirements, value added created and others. In such case an investment fund could be conceived as expenditure on goods and services, including labor, from the other sectors and if so it could be thought of as increases in the demand for those goods and thus we can, through the above mentioned coefficients, trace their effects. (2) As can be seen the inputs required for such investments will not be the type designed to satisfy the consumers needs directly but rather through being an

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- (1) This fact will be referred to in a later article when we discuss the iterative method of solving an input-output problem.
 - (2) This point will be examined in greater detail later when we discuss the application of the table to certain problems in Egypt.

Inputs needed for this include in the final demand for industrial goods



The direct input for the increase in final demand for industrial goods.

The indirect input requirements for the increase in Final Demand for Industrial Goods.

essential part for the production of the finished goods. In this case, the application of such 'criteria as the income elasticity of demand in order to predict the requirements for such commodities would be extremely difficult and may even be inconceivable. The input-output table, on the other hand, provides us with a particularly suitable device for such prediction. This is due, of course to the very nature of the table which does not overlook the complexity of the relationships among the different sectors but rather emphasizes it. The coefficients of "direct and indirect requirements" in this case are the only answer. The table could inform us also of the repercussions of certain government policies, such as increase in taxation, more government investment or increase in public works. All these actions could be conceived as having direct effects on the demand for the different commodities and their repercussions on the different sectors of the economy could thus be determined. As will be described in a later article in greater details the input-output table provides us with unique tool for calculating the effects of an import substitution policy. This is of paramount importance particularly in a developing country where industrialization generally tends to substitute imports by local production. In this case it is extremely important to calculate the net savings in imports which such policy may lead to. (2) This could be easily done through the input-output table as it enables us to calculate the direct and indirect requirement of imports for any particular demand. In short, the input-output method is most suited for solving the problems where the complex characteristic of interdependency is involved.

The input-output model and the concept of national income accounts

Those who are familiar with national income accounts and its underlying concepts will feel at home when being introduced to the input-output method. They both provide us with a system of accounts which cover the whole economy and, in fact, they are complementary to each other. However, there is a basic difference between the two methods, the reason for which could be traced to the ultimate purpose which each aims to serve. As for national income accounts, it aims at measuring the value of goods and services produced by the entire economy within a specified period of time, normally one year. The national income accountant, therefore, is interested in the final results of the economic activities and hence, he only considers the net effects of all the dealings which take place within the economy. To do that he avoids double counting and therefore deliberately disregards transactions between the different productive sectors. It is there, in fact, where the basic difference between that method of accounting and the input-output method lies. The latter being a main body of the interindustry analysis which concerns itself mainly with

(2) This adoption of such method may be offered as a good tip to the economists of the Ministry of Industry. The indirect effects are so important that they should be taken into account.

the interrelations arising from production, attaches a distinct importance to the flow of goods and services from one productive sector to the other. It is this interdependence among the different sectors which the input-output table aims to bring to the limelight and in doing that double counting becomes an accepted phenomenon. Also as we indicated before the input-output model is most helpful in dealing with the problems where the structural interdependency is the crucial factor and where the more simplified framework of national income accounts could be of very little help.

To illustrate the relationship between the input-output table and the national income accounts we have utilized the data of the 1954 input-output table for the Egyptian Economy to construct the three tables given below. Table 1 shows clearly how in calculating the G.N.P. we avoided double counting. In both sides of the table our starting point was the gross value of production. In the left side the value added in the three sectors was calculated simply by subtracting from the gross value of production in each sector, the value of inputs required for the production of that sector. For instance the value of any particular input, say industrial goods has to be subtracted from the value of the gross production of the sector which consumed it as it has already been calculated in the production of its own sector. This fact leads us to realize how in measuring the G.N.P. we are really more concerned with the value of the final goods produced by the whole economy. This end could be pursued by constructing an account similar to that given in the left side of Table 1 which shows the value of the sales of every sector to final demand purposes. As it is clear this was reached at by subtracting from the gross value of production from each sector that part of its production which was sold for intermediate consumption purposes. If we add up the value added from the three sectors which appear in the left side of the table and also add the final sales from the three sectors which appear in the right side of the table we should find that the two totals are equal. However, this is not so in our example (1) simply because we have to deal with imports and also with a certain portion of the value added which appear in the final demand sectors of the input-output table, i.e. Table 2. In fact we had to follow this course in order to show how the figures in our three tables are related and how the gross national product could be calculated from them. Now in order to equate the two sides of Table 1 we should add to the total of the value added in the three sectors the part of the value added which appear in the input-output table within the final demand sectors. This will give us a total of value added of 1,054,109.(2) As regards the left side of the table we should add to the total of the final sales the value of the imports needed for final demand purposes and also the same figure of value added which appear in the final demand columns of the input-output table.

(1) An illustrative example with no imports involved could be constructed to show the total of the value added is equal to the final sale.

(2) This figure is in thousand Egyptian pounds. In other words it means 1,054 million pounds.

TABLE 1

GROSS NATIONAL INCOME		(Figures in thousand Egyptian Pounds)	
AGRICULTURE		AGRICULTURE	
Gross Production	400,814	Gross Production.....	400,814
Inputs from		Intermediate Sales to	
Agriculture ...	47,481	Agriculture ...	47,481
Industry	15,170	Industry	205,790
Services	148,734	Services.....	92
Imports	16,500		<u>253,363</u>
	<u>227,885</u>		
Value Added.....	<u>172,929</u>	Final Sales	<u>147,451</u>
	=====		=====
INDUSTRY		INDUSTRY	
Gross Production.....	898,765	Gross Production	898,765
Inputs from		Intermediate Sales to	
Agriculture ..	205,790	Agriculture ...	15,170
Industry.....	253,615	Industry	253,615
Services.....	99,358	Services	48,288
Imports	66,966		<u>317,073</u>
	<u>625,729</u>		
Value Added	<u>273,036</u>	Final Sales	<u>581,692</u>
	=====		=====
SERVICES		SERVICES	
Gross Production.....	554,561	Gross Production	554,561
Inputs from		Intermediate Sales to	
Agriculture ..	92	Agriculture ...	148,734
Industry	48,288	Industry	99,358
Services	28,659	Services	28,659
Imports	7,313		<u>276,751</u>
	<u>48,352</u>		
Value Added.....	<u>470,207</u>	Final Sales.....	<u>277,810</u>
	=====		=====
Total Value added in the three Sectors	916,172	Total Final Sales. 1.006,953	
+ Value added in the final demand Sectors.....	137,935	+ Imports for	
TOTAL Value Added (Gross National Income)	<u>1,054,109</u>	Final demand ..	82,105
	=====	+ Value added in the final demand sectors	<u>137,935</u>
		- Total Value of Final demand imports....	<u>172,884</u>
		(Gross National Product).	<u>1,054,109</u>
			=====

And then we should subtract the total of imported goods. In other words we try to reach a figure which represents the value of goods and services which were available for final demand and then by subtracting the amounts of imports from it we can reach a figure which represents the gross national product which appears on the left side to be also 1,054,109.

However before leaving Table 1, the reader's attention should be attracted to the fact that there should not necessarily be a certain correspondence between the value added in each sector and the sectors contributing to the bill of final goods that is despite the fact that the total of the value added from all sectors should equal the total of the final sale of goods and services after subtracting the value of imports. In fact it often happens that a sector may have a large contribution to the gross national product at the time when its contribution to final demand is of minor importance. This is largely the case with industries producing intermediate goods.(1)

As a contrast to table 1, table 2 shows how the interdependency among the different sectors of the economy form an integral part of the formation of an input-output table. The deliveries among these sectors stand clear and double counting becomes permissible, in fact deliberate. In order to reach the gross production from the agricultural sector we add up the amount of that production which went to intermediate consumption and that which went to final demand. This is despite the fact that the value of the part of the agricultural production which went to intermediate consumption will form an integral part of the production of the sector which consumed it and thus will be embodied again in the value of its production. It is therefore obvious that the total of the column of gross production in table 2, is not to be compared with the total of the final sales which appear in the right side of table 1. In fact it is the total of the column of final demand after deducting the total amount of imported goods that should be compared with the total given in the right side of table 1 as they both indicate the amount of gross national product by use. In the meantime the gross national product by source of origin appears in table 2 as the row of value added which could be compared to the total of value added given on the left side of table 1. The correspondence between the column of final demand and the row of value added in table 2 could be easily illustrated by the following equation

$$\sum_i Y_i - \sum_j M_j = \sum_j V_j \quad (4)$$

where Y_i is the final demand for commodity i and M_j is the inputs from imports to sector j and V_j is the value added in sector j . Using this equation we get

$$1,226,993 - 172,884 = 1,054,109$$

which is the gross national product and exactly the same figure which we arrived at in table 1.

(1) This point will be handled in more details when we discuss the characteristics of the Input-Output table.

To conclude this parallel which we tried to draw between the input-output table and the national income accounts table 3 is presented. It shows how input-output data could be arranged in national accounts form. It also makes clear how the idea of interdependency among the productive sectors is thrown in the background by grouping all those sectors in one, the business sector. The rest of the table comprise other sectors which are traditionally used in national accounting. These sectors give breakdowns of final use and primary inputs. As it is the case with the previous tables, the gross national product could be calculated simply by utilizing equation 4. According to table 3 the total of final demand would be

$$156,279 + 189,570 + 757,155 + 123,989 = 1,226,993$$

utilizing the above equation we get

$$1,226,993 - 172,884 = 1,054,109$$

which is the same figure as that which we got from the other tables. The above tables however give emphasis to complementary nature of the two systems of accounts.

The general characteristics of an input-output table

So far we have been talking about the input-output table in general terms. But in order to have a better grasp of the underlying concepts of that table and to be able to follow later on the mathematical interpretations of these concepts it is essential to examine more closely its general characteristics. For this purpose we present table 4 which is an aggregation of the 1954 input-output table for the Egyptian Economy.⁽¹⁾ The input-output accounts are a form of double-entry book-keeping the main function of which is to record the transactions between the different sectors of the economy. We could, therefore, say that the concept of a sector is a corner stone in the input-output analysis. For this purpose a sector may be an industry, a household or any sort of economic entity which would be able, because of its functional characteristic to receive inputs from other sectors and also to deliver outputs to other sectors or to the rest of the world. These transactions are generally flows of goods or services from one sector to the other and they are generally attributed to a certain period of time and related to a certain production. They could also be measured in physical terms, i.e. (tons, bushels, etc.) or in value terms, i.e. (dollars, pounds). As regards the transactions in all the tables in this book they are given in value terms and in that we are following a general tradition set by Professor Leontief. This procedure, of course, has its own merits and will be appreciated later when we consider the mathematical interpretation of the input-output table. However, it is generally the case that most of, if not all,

(1) This table was constructed by the input-output unit, which is part of the National Planning Committee, Cairo, Egypt.

AN AGGREGATED INPUT-OUTPUT TABLE FOR EGYPT, 1954.

Table 2

(In Thousand £.E.)

Purchasing Sector Producing Sector	Agriculture	Industry	Services	Final Demand	Gross Production
Agriculture	47,481	205,790	92	147,451	400,814
Industry	15,170	253,615	48,288	581,692	898,765
Services	148,734	99,358	28,659	277,810	554,561
Imports	16,500	66,966	7,313	82,105	172,884
Total Inputs	227,885	625,729	84,352	1,089,058	2,027,024
Value Added	172,929	273,036	470,209	137,935	1,054,109
Total Output	400,814	898,765	554,561	1,226,993	3,081,133

of the initial data which are used in the construction of the input-output table are in physical units. In evaluating these physical units, producers' prices are generally used with all trade margins and transportation margins being grouped in separate sectors, and allocated to the using sectors. However purchasers' prices could also be used. Although some maintain that they produce less satisfactory results. Moreover the input-output table is based on the accounting identity that the total deliveries from every sector are equal to the total inputs used by that sector. This means that the total output of a sector should correspond to the total input including those from primary factors to that sector.(1) As we will see later this is not particularly true on the sectoral level in the case of final demand and primary factors nevertheless their aggregates, by definition, should be the same.

The data, as we can see from table 4, are arranged in a checker-board table in which each sector is represented both by a row and a column. This is particularly true for the productive sectors or those which consume intermediate goods in order to execute its function which is the production, either of other intermediate goods or goods for final use. In the case of table 4 those sectors are 7 and in this case the table could be described as being of the order of 7X7. These sectors form actually the main body of the table and they are often referred to as the interflow matrix. Larger number of sectors could be included in this interflow matrix but their number could be conceived as a function of the availability of the required data as well as the level of disaggregation desired to suit the type of analysis we have in mind. Quite often tables are prepared with more rows of this type than columns and in this case the table is referred to as a rectangular table and it is most useful if we desire greater details of the inputs.(2) The original 1954 table for Egypt is of the order of 83X83 and that for 1959 is of the order of 33X33.

If we read along the rows, the figures indicate the distribution of the output of the sectors and if we read along the columns the figures indicate the inputs required by each sector. However, before attempting to read along the rows and columns it may be of some help to divide the table into quadrants, each containing a number of sectors which are at least of homogeneous accounting characteristics. To start with we can group together sectors 1 to 7 and let us call it quadrant 1. Those sectors will be called the productive sectors simply because they are the sectors which perform the productive operation, and in this sense they form the main body of the interindustry accounts. In executing this function they need inputs not only from themselves but also from imports and other primary inputs. At this point it is important to emphasise the difference between the inputs from the productive sectors or what are often called the "produced inputs" and the "primary inputs" as this will have a significant influence on the solutions of the input-output problems. As for the first type of inputs they are

(1) The underlying wisdom of the idea that the total output of every sector should correspond to the total input to that sector will be discussed later.

(2) Reference will be made later to the usefulness of constructing such tables and the methods of solution.

THE 1954 INPUT-OUTPUT DATA AGGREGATED IN NATIONAL ACCOUNTS FORM.

Table 3

(Figures in Thousand £.E.)

Purchasing Sector Producing Sector	Business	Government	Foreign Trade (Exports)	Household Consumption	Gross Investment	Total Receipts
Business	847,187	49,784	189,570	669,474	98,125	1,854,140
Government	175,030	-	-	10,432	-	185,462
Foreign Trade (Imports)	90,779	7,277	-	48,964	25,864	172,884
Households	741,144	99,218	-	28,285	-	868,647
Total Payments	1854,140	156,279	189,570	757,155	123,989	3,081,133

the kind of inputs which are produced by the productive sectors themselves and there is a definite relationship between their production and the inputs required for that operation. These inputs are the ones which will be considered later in the solution of the model particularly when we want to arrive at the indirect effects of a certain final bill of goods. As for the primary inputs they are called so simply because they are not produced within the system. For instance imports are considered so because they are produced in other countries and their production does not represent any claims on the resources of the economy. Equally true they do not have indirect effects because they are not produced within the system and do not require any inputs. Consequently in solving for the amounts of imports needed for the production required to satisfy a final bill of goods, we will not have to worry about those indirect effects which we generally consider when we deal with the produced inputs. But the main type of primary inputs are those which are grouped in row No. 10 and called value added. They are called so because they are the difference between the gross production and the total inputs required for that production. A breakdown of this row will show inputs of labor, profits on capital and other item which compose what we called the value added. Finer breakdowns could be achieved and this of course depends on the type of analysis we have in mind. If we are interested in calculating the labor requirements for a certain investment program then labor inputs in the shape of wages should be made distinct. Similarly if we are interested in the distributed ownership income then this should appear as separate inputs and so on. Like inputs from imports these inputs are produced exogenously from the system; also there is not definite relationship between the supply of such inputs and a certain set of inputs as it is the case with produced inputs. The supply of labor for instance is not produced through the purchase of the working force and so it is the case with the rest of the primary inputs. If we group row 8 & 10 and stop at column 7 this will give quadrant 11 which shows the inputs of primary factors into the productive sectors.

As we have sectors which show the supply of the primary factors we have others on the demand side which could be referred to as primary sectors or generally known as the final demand sectors. They are considered primary sectors because the inputs purchased by them do not physically produce their output and consequently we find that these inputs do not vary proportionally to the outputs of these sectors. This is particularly true of the government sector and household. These form the columns 9 to 14 and they are different from the productive sectors (columns 1-7) in that the purchases of the former represent the ultimate goal of the economic system while the activities of the latter sectors are a means for achieving that goal. The figures appearing in these columns represent those goods and services which went for final use during the accounting period. In this table the final demand sectors are only 6 but finer breakdown of these sectors are sometimes desirable. For instance the sector investment could be broken down to different types of investments. The reason for that of course is that every investment has its particular input structure. This is particularly important if we desire to study the effects of different types of investment on

imports, employment, production requirements, etc. It is also an essential step for constructing a capital matrix and of paramount importance in investment programming in general. Similarly the sector exports could be broken down to exports to different countries. This is particularly important in a country with limited supply of hard currencies. In this case it may be useful to distinguish between exports to the hard currency areas and exports to other areas. It is equally important if we are constructing a table which shows regional trade.

As it is the case with the productive sectors these sectors receive inputs from the productive sectors and from the primary inputs sectors. The primary inputs in this case appear in our table under only two sectors, household consumption and government consumption and they represent domestic help in the first and government salaries in the second. To complete the division of our table let us call quadrant III that which includes the primary inputs into the final demand sectors that is the quadrant which comprises the cells from rows 8 & 10 and columns 9-14. Let us also call quadrant IV that which includes the inputs from the productive sectors into the final demand sectors, i.e. the quadrant which includes the cells from rows 1-7 and columns 9-14.

From the above we can see that the input-output table is distinctly divided into four sections or as we called them, quadrants. This, in fact, underlines the basic design of this type of interindustry accounts which is derived by dividing the demand for commodities into intermediate and final and the inputs into produced and primary. The first distinction is sometimes (1) paralleled with that which is made in Keynesian income analysis between "induced" and "autonomous" elements. In the case of the input-output model the induced elements are those which are included in quadrants I and II. They are called so because their magnitudes depend on the autonomous part of the table. As we indicated before the sector to be included in the autonomous section of the input-output table and the breakdown of these sectors depend largely on the type of analysis we have in mind. Table 4 is in conformity with what is known as the open Leontief model and as we mentioned before it is called so because of the fact that the magnitudes of the final demand sectors are autonomously decided upon or they are given. On the other hand when $\sum_i Y_i = 0$ or in other words when all the autonomous elements are included within the induced part of the model then it is described as being a closed one. This type of model is generally discussed under dynamic models and a great deal of work was done in this field by Professor Leontief and his assistants at the Harvard Economic Research Project. (2) Sometimes, however, only part of these autonomous demand sectors are included in the interflow matrix (quadrant I) and in this case they become part of the induced elements of the model and their magnitudes will be derived then from the solution of the model rather than exogenously of it. A typical example of this would be the inclusion of household consumption which would be represented in the interflow matrix by a column and a corresponding row which shows household income and in this case a certain definite

(1) Chenery and Clark, "Interindustry Economics", p. 15

(2) See W.W. Leontief, "Studies in the Structure of the American Economy", 1952.

relationship is assumed between household consumption and household income. Of course the number of such sectors to be included in the autonomous part will always depend on the type of analysis we have in mind.

From the above description of the table we can also see that the input-output model is based on the idea that a fixed set of inputs are required for the production of each sector and that these inputs vary proportionately to the size of production. However this is only true in the case of the productive sectors which are included in quadrant I. And if this is so then inputs to every sector will be expressed as ratios to the total value of the production of that sector. Moreover we can see that the input-output model is based on the idea that the total outputs of every sector will be equal to the total inputs to that sector including the primary ones. Again this is only true in the case of the productive sectors and although the aggregate totals of the primary inputs including imports should by definition equal the aggregate of the final demand columns yet this is not so on the sectoral level. In fact the primary input row (only row No. 9) shows the gross national product by sector of origin and the final demand columns (excluding the value of imports) show the gross national product by destination. As for quadrant I it shows all the intermediate transactions and any figure in it could be looked upon in two ways. If we read along the column the figure would indicate that the sector in question has bought this amount from the sector which is represented by the row which corresponds to that figure. On the other hand if we read along the row the same figure would indicate that the sector which is represented by that row has sold the indicated value of input to the sector represented by the column which corresponds to that figure. The total of quadrant I would indicate the amount of intermediate consumption from domestic production and if we add the total inputs from imports to the productive sectors this will give us the total intermediate consumption which was required for the total production in the economy which appear as the total of column 16. Similarly the figures appearing in column 8 indicate the total intermediate sales from the corresponding row to the productive sectors and if we add each of these figures to its corresponding figure in column 15 which shows the total delivery from the corresponding row to the final demand sectors then we get figures which represent the gross production for every row. These are included in column 16.

Besides its valuable analytical use the input-output model presents a system of national accounting which in many senses is superior to that of the national income accounting. Moreover the particular framework of the input-output model largely facilitates the use of a wide variety of data and the mere fact that the totals of each column should be equal to the corresponding row provides a check on the consistency of the data on specific levels rather than that which is achieved merely by equating the overall total of income and production as it is the case in the National Income Accounting. My experience in the field of the construction of the input-output table showed me how the attempt to construct such tables reveal the numerous gaps in the available data, gaps which should be filled if a better understanding of the economy could be achieved.

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