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Effect of water density on the response of Square Tension Leg Platform

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Abstract— tension-leg platform (TLP) or extended tension leg platform (ETLP) is a vertically moored floating structure normally used for the offshore production of oil or gas, and is particularly suited for water depths greater than 300 metres and less than 1500 metres. The platform is permanently moored by means of tethers or tendons grouped at each of the structure's corners. A group of tethers is called a tension leg. A feature of the design of the tethers is that they have relatively high axial stiffness (low elasticity), such that virtually all vertical motion of the platform is eliminated. This allows the platform to have the production wellheads on deck (connected directly to the subsea wells by rigid risers), instead of on the seafloor. This allows a simpler well completion and gives better control over the production from the oil or gas reservoir, and easier access for down hole intervention operations. In this paper a numerical study for a square TLP using modified Morison equation was carried out in the time domain with water particle kinematics using Airy's linear wave theory to investigate the effect of changing water density on the mass matrix of TLP's and the dynamic behavior of TLP's. The effect was investigated for different parameters of the hydrodynamic forces such as wave periods, and wave heights. The numerical study takes into consideration the effect of coupling between various degrees of freedom. The stiffness of the TLP was derived from a combination of hydrostatic restoring forces and restoring forces due to cables. Nonlinear equation was solved using Newmark's beta integration method. Only uni-directional waves in the surge direction was considered in the analysis.

Keywords—density, square tension leg platforms, hydrodynamic wave forces, wave characteristic.

A

II. INTRODUCTION

type of floating production system, tension leg platforms (TLPs) are buoyant production facilities vertically moored to the seafloor by tendons. While a buoyant hull supports the platform's topsides, an intricate mooring system keeps the TLP in place. The buoyancy of the facility's hull offsets the weight of the platform, requiring clusters of tight tendons, or tension legs, to secure the structure to the foundation on the seabed. The foundation is then kept stationary by piles driven into the seabed. The tension leg mooring system allows for horizontal movement with wave disturbances, but does not permit vertical, or bobbing, movement, which makes TLPs a popular choice for stability,

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such as in the hurricane-prone Gulf of Mexico. The basic design of a TLP includes four air-filled columns forming a square. These columns are supported and connected by pontoons, similar to the design of a semisubmersible production platform. Nonetheless, since their inception in the mid 1980s, TLP designs have changed according to development requirements. Now, designs also comprise the E-TLP, which includes a ring pontoon connecting the four air-filled columns; the Moses TLP, which centralizes the four-column hull; and the SeaStar TLP, which includes only one central column for a hull. The platform deck is located atop the hull of the TLP. The topside of a TLP is the same as a typical production platform, consisting of a deck that houses the drilling and production equipment, as well as the power module and the living quarters. Dry tree wells are common on TLPs because of the lessened vertical movement on the platforms. Most wells producing to TLPs are developed through rigid risers, which lift the hydrocarbons from the seafloor to dry trees located on the TLP deck. Many times, steel catenary risers are also used to tie-in the subsea flow lines and export pipelines. The third-most used type of floating production facility in the world, TLPs are ideal for a broad range of water depths. Currently, there are three different types of TLPs: full-size TLPs, mini TLPs and wellhead TLPs. Most of the literature available Paulling and Horton [6] reported a method of predicting the platform motions and tether forces due to regular waves using a linearized hydrodynamic synthesis technique. Each member was assumed to be cylindrical in shape with cross-sectional dimensions small in comparison to both the length of the cylinder and the wave length. Ahmad et. al, [2] studied the effect of the variable submergence on the maximum tether tension force on TLP with change in wave incidence angle. The study was carried out on coupled and uncoupled model. Jain [5] dynamic response analysis of a TLP to deterministic first order wave forces is presented, considering coupling between the degrees-of-freedom (surge, sway, heave, roll, pitch and yaw). The analysis considers nonlinearities produced

due to changes in cable tension and due to nonlinear hydrodynamic drag forces. The wave forces on the elements of the pontoon structure are calculated using Airy's wave theory and Morison's equation ignoring diffraction effects. The nonlinear equation of motion is solved in the time domain by Newmark's beta integration scheme. The effects of different parameters that influence the response of the TLP are then investigated. Like change in tether tension force and damping ratio. Chan K. Yang, M. H. Kim [4] developed a numerical study of the transient effect of tendon disconnection on global performance of an extended tension leg platform (ETLP) during harsh environmental conditions of Gulf Of Mexico (GOM). A.M.Abou-Rayan, Ayman A. Seleemah, and Amr R. El-gamal [1] developed a numerical study on determining the dynamic responses of TLPs subjected to regular wave. They found that coupling between various degrees of freedom has insignificantly dependent on the wave height; whereas for longer wave periods of 15 sec. Amr R. El-gamal, Ashraf Essa [3] developed a numerical study to investigate the effect of tethers length and wave characteristics such as wave period and wave height on the response of TLP's. they found that for short wave periods (i.e. 10 sec.), the surge response consisted of small amplitude oscillations about a displaced position that is significantly dependent on tether length, wave height; whereas for longer wave periods, the surge response showed high amplitude oscillations about that is significantly dependent on tether length. Amr R. El-gamal, Ashraf Essa [4] developed a numerical study to investigate the effect of tethers tension force and wave characteristics such as wave period and wave height on the response of TLP's. they found that for short wave periods (i.e. 10 sec.), the surge response consisted of small amplitude oscillations about a displaced position that is significantly dependent on tether length, wave height; whereas for longer wave periods, the surge response showed high amplitude oscillations about that is significantly dependent on tether tension force.

In this paper, a numerical study was conducted to investigate the dynamic response of a square TLP (shown in Fig. 2) under hydrodynamic forces considering all degrees of freedom of the system (shown in Fig. 1). The analysis was carried out using modified Morison equation in the time domain with water particle kinematics using Airy's linear wave theory to investigate the effect of changing the water density on the mass matrix of TLP's and the dynamic behavior of TLP's.. The effect was investigated for different parameters of the hydrodynamic forces such as wave periods, and wave heights. The numerical study takes into consideration the effect of coupling between various degrees of freedom. The stiffness of the TLP was derived from a combination of hydrostatic restoring forces and restoring forces due to cables and the nonlinear equations of motion were solved utilizing Newmark's beta integration scheme. The effect of wave characteristics such as wave period and wave height on the response of TLP's was evaluated. Only uni-directional waves in the surge direction was considered in the analysis.

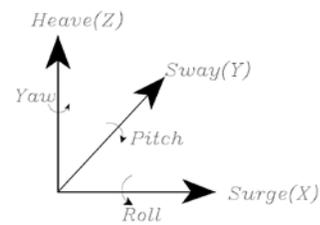


Fig.1. Six degree of freedom of offshore structure.

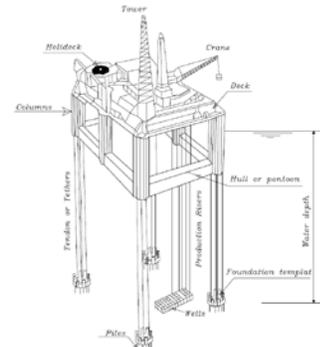


Fig.2. Tension leg platform scheme

II. STRUCTURAL IDEALIZATION AND ASSUMPTIONS

The general equation of motion of the square configuration TLP model under a regular wave is given as

$$[M]\{x''\} + [C]\{x'\} + [K]\{x\} = \{F(t)\} \quad (1)$$

where, $\{x\}$ is the structural displacement vector, $\{x'\}$ is the structural velocity vector, $\{x''\}$ is the structural acceleration vector; $[M]$ is the structure mass matrix; $[C]$ is the structure damping matrix; $[K]$ is the structure stiffness matrix; and $\{F(t)\}$ is the hydrodynamic force vector.

The mathematical model derived in this study assumes that the platform and the tethers are treated as a single system and the analysis is carried out for the six degrees of freedom under different environmental loads where wave forces are estimated at the instantaneous equilibrium position of the platform utilizing Morison's equation and using Airy's linear wave theory. Wave force coefficients, C_d and C_m , are the same for the pontoons and the columns and are independent of frequencies as well as constant over the water depth. The following assumptions were made in the analysis.

- 1) Change in pre-tension is calculated at each time step, so the equation of equilibrium at each time step modifies the elements of the stiffness matrix.
- 2) The platform has been considered symmetrical along the surge axis. Directionality of wave approach to the structure has been ignored in the analysis and only a uni-directional wave train has been considered.
- 3) The damping matrix has been assumed to be mass and stiffness proportional.
- 4) The force on tethers (gravity, inertia, and drag, hydrostatic and hydrodynamic forces) has been neglected because of its small area and also the tether curvature is not

- significant in motion; only the axial forces acting on tethers have been considered.
- 5) Hydrodynamic forces on connecting members and mooring legs have been neglected.
 - 6) The wave, current and structure motions are taken to occur in the same plane and in the same direction, the interaction of wave and current has been ignored.
 - 7) Integration of hydrodynamic inertia and drag forces are carried out up to the actual level of submergence, when variable submergence is considered.

- 4) The coefficient for heave stiffness matrix doesn't depend on tether tension force while the surge coefficient directly proportion to tether tension force and inverse proportion to tether length.

III. DEVELOPMENT OF A SQUARE TLP MODEL

A. Draft Evaluation

At the original equilibrium position, Fig. 3, summation of forces in the vertical direction gives:

$$W + T = F_B \quad (2)$$

We find that

$$D_r = \frac{[\{(W + T) / (0.25 \rho \pi g)\} - (2D_p^2 s_a) - (2D_p^2 s_b)]}{4D_c^2} \quad (3)$$

where, F_B is the total buoyancy force; W is the total weight of the platform in air; T is the total instantaneous tension in the tethers; T_o is the initial pre-tension in the tether; p is the mass density of sea water; D_c is the diameter of TLP columns; D_p is the diameter of pontoon; S_a and S_b are the length of the pontoon between the inner edges of the columns in the x and y directions, respectively; and D_r is the draft.

We notice from eq. (3) that drift distance inversely proportion to water density.

B. Stiffness Matrix of Triangular TLP Configuration

The stiffness of the platform is derived from a combination of hydrostatic restoring forces and restoring forces due to the cables. Restoring force for motions in the horizontal plane (surge, sway, and yaw) are the horizontal component of the pretension in the cables, while restoring forces for motions in the vertical plane arise primarily from the elastic properties of the cables, with a relatively small contribution due to hydrostatic forces.

For more detailed about the derivation of the stiffness matrix, the reader is referred to [1]

The overall stiffness matrix shows:

- 1) The presence of off-diagonal terms, which reflects the coupling effect between the various degrees of freedom.
- 2) The coefficients depend on the change in the tension of the tethers, which is affecting the buoyancy of the system. Hence, the matrix is response dependent.
- 3) Hence, during the dynamic analysis, the $[K]$ matrix is not constant for all time instants, but its components are continuously changing at each time step depending upon the response values at the previous time step.

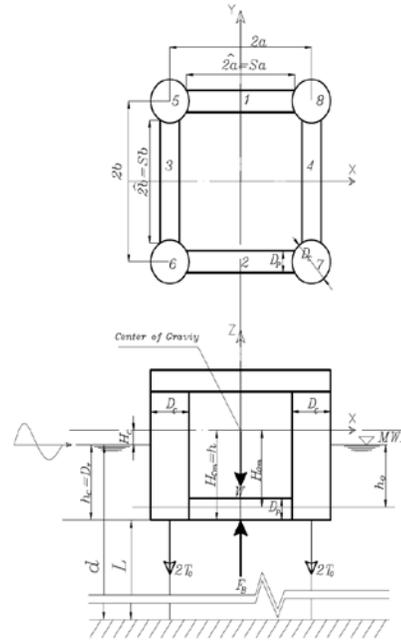


Fig. 3 The Square TLP (plan and elevation)

C. Mass Matrix, $[M]$

The mass matrix is assumed to be lumped at each degree of freedom. Hence, it is diagonal in nature and is constant. However, the added mass, M_a , due to the water surrounding the structural members has been considered up to the mean sea level (MSL) and arising from the modified Morison equation. The presence of off diagonal terms in the mass matrix indicates a contribution of the added mass due to the hydrodynamic loading. The fluctuating components of added mass due to the variable submergence of the structure in water is considered in the force vector depending upon whether the sea surface elevation is above or below the MSL. The loading will be attracted only in the surge, heave and pitch degrees of freedom due to the unidirectional wave acting in the surge direction on a symmetric configuration of the platform about the x and z axes.

For more detailed about the derivation of the mass matrix, the reader is referred to [1]

D. Structural Damping $[C]$

Structure Damping was presented in the form of mass matrix is assumed to be mass and restoring force proportional,

$$c = m \left(\sum_{n=1}^{n=6} \frac{2\zeta_n \omega_n}{M_n} \phi_n \phi_n^T \right) m \quad (4)$$

Where; $\{\phi_n\}$ and ω_n are the mode shapes and structure's natural frequencies, ζ_n is the structural damping ratio, C is the

damping matrix, m is the total structure mass matrix and M_n is the corresponding element of the $\{\emptyset_n\}^T [m] \{\emptyset_n\}$

This matrix is calculated based on the initial values of $[K]$ and $[M]$ depending on the type of the platform.

E. Hydrodynamic Force Vector, $\{F(t)\}$ on square TLP

The hydrodynamic force vector is calculated in each degree of freedom according to modified Morison's equation which takes into account the relative velocity and acceleration between the structure and the fluid particles. It is also worth mentioning that the ratio d/H can be related to d/λ . Based on the limiting heights of breaking waves, it become unstable and break when $H/\lambda \geq 0.1$, (H is the wave height and λ is the wave length).

For the uni-directional wave train in the surge direction, the force vector $\{F(t)\}$, is given by

$$F(t) = \{F_{11} \quad F_{21} \quad F_{31} \quad F_{41} \quad F_{51} \quad F_{61}\}^T \quad (5)$$

Since the wave is unidirectional, there would be no force in the sway degree-of-freedom F_{21} and hence there will be no moment in the roll degree of-freedom F_{41} . Because of the vertical water particle velocity and acceleration, the heave degree-of-freedom would experience wave force F_{31} . The force in the surge direction F_{11} on the vertical members will cause moment in the pitch degree-of-freedom F_{51} . However, forces in the surge degree-of-freedom are symmetrical about the X axis (due to the symmetry of the platform to the approaching wave) and there will be no net moment caused in the yaw degree-of-freedom F_{61} .

For more detailed about the derivation of the force vector, the reader is referred to [1]

F. Solution of the Equation of Motion in the Time Domain

The equation of motion is coupled and nonlinear and can be written as

$$[M]\{x''(t+\Delta t)\} + [C]\{x'(t+\Delta t)\} + [K]\{x(t+\Delta t)\} = \{F(t+\Delta t)\} \quad (6)$$

Equation (6) is nonlinearly coupled, because of the presence of structural displacement, velocity and acceleration in the right hand side of the equation. Therefore, the force vector should be updated at each time step to account for the change in the tether tension. To achieve this response variation a time domain analysis is carried out. The Newmark's beta time integration procedure is used in a step wise manner. This procedure was developed by Newmark together with a family of time-stepping methods. The following values are updated

- 1) Stiffness coefficients which vary with tether tension.
- 2) Added mass which varies with sea surface fluctuations.
- 3) Wave forces at the instantaneous position of the displaced structure.

IV. RESULTS AND DISCUSSION

A numerical program was developed using MATLAB software where solution based on Newmark's beta method was

obtained. The studied TLP geometrical, physical and the mechanical properties of the tethers are shown in Table I.

The main dynamic charchatrstric of the system chosen in the study are given in table II, Such as natural period of the triangle TLP

It can be note from table II that square TLP has a high natural period in horizontal plan where as small natural period in vertical direction.

Also, it can be seen that changing the water density has a valuable effect on the natural period of horizontal movement (surge, sway and yaw movement)

While has little effect on the natural period on the movement in the vertical direction that is heave, roll and pitch

TABLE I
GEOMETRIC PROPERTIES OF THE SQUARE TLP AND LOAD DATA

Water properties	
Gravity acceleration (m/sec ²)	9.81
Water weight density (kN/m ³)	12.45,11.35 and 10.25
Inertia coefficient, C_m	1.5
Drag oefficient, C_d	0.9
Current velocity (m/sec), U_c	0
Wave period (sec), T_w	10 and 15
Wave height (m), H_w	8 and 10
Platform properties	
Platform weight (KN), W	330100
Platform length (m), P_1	76.77
Platform radius of gyration in x-directions (m), r_x	35.2
Platform radius of gyration in y-directions (m), r_y	35.2
Platform radius of gyration in z-directions (m), r_z	42.5
Tether total force (KN), T	135600
Tether area (m ²)	0.5
Draft (m)	13.7,19.53 and 26.58
Tether modulus of elasticity (kn/m ²), E	2.2e7
Diameter of columns (m), D_c	14.1
Diameter of pontoon (m), D_p	12.1
Center of gravity above the keel (m), h	27.5
Water depth (m), d	300
Damping ratio, ζ	0.02

TABLE II
CALCULATED NATURAL STRUCTURAL PERIODS FOR DIFFERENT ANALYSIS CASES (IN SECONDS)

DOF	Analysis Case		
	Water density 12.45Kn/m ³	Water density 11.35Kn/m ³	Water density 10.25Kn/m ³
Surge	63.4	63.28	62.99
Sway	63.4	63.28	62.99
Heave	1.15	1.12	1.09
Roll	1.04	1.02	0.99
Pitch	1.04	1.02	0.99
Yaw	48.39	49.1	49.64

A. Surge Response

The time histories of the surge responses for the sqaure TLP are shown in Figs. 4 to 7. It is observed that, for a specific wave period, the amplitude of oscillations increases as the wave height increases. For short period the system responds in

small amplitude oscillations about a displaced position that is dependent to wave height and water density. The amplitude of oscillations increases with the increase in the wave period, which is expected because as the wave period increases, it becomes closer to the surge natural period of vibration (about 150 sec.). Moreover, in all cases, the surge response seems to have periodic oscillations that have the same exciting wave period [3].

The effect of water density is obvious in Figs. 4 to 7 which indicate that it affect the drift value of the displaced position. As water density becomes bigger the drift decreases but the water density has little effect on the amplitude of the oscillation. Finally, the transient state takes about 100-120 seconds where the stationary state begins.

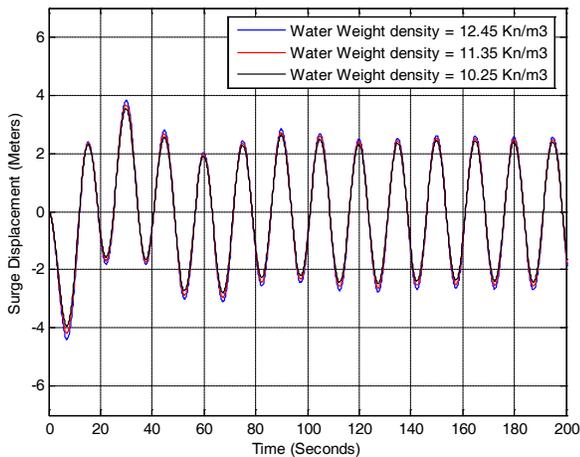


Fig. 4 Coupled Surge response of square TLP for Wave Height = 8 m and wave period = 15 sec

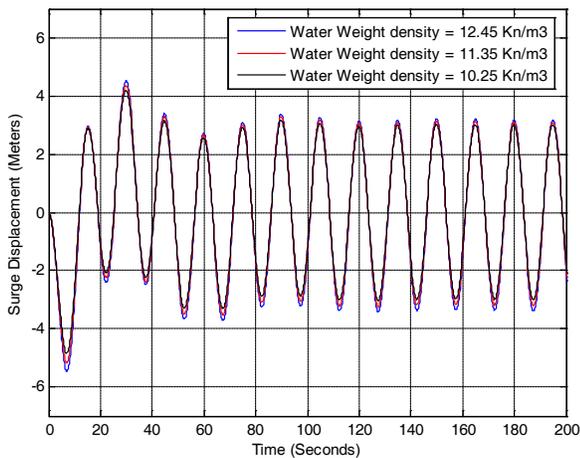


Fig. 5 Coupled Surge response of square TLP for Wave Height = 10 m and wave period = 15 sec.

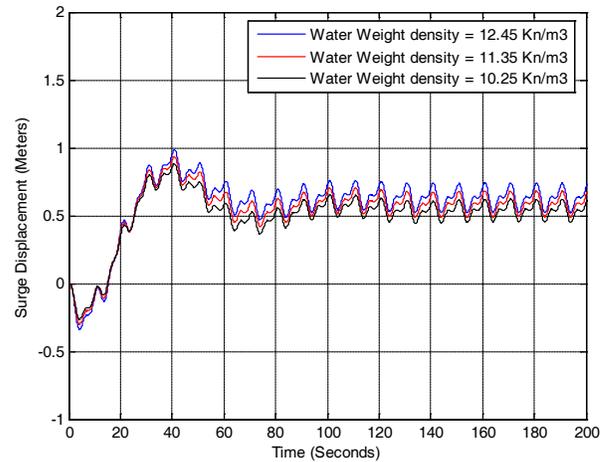


Fig. 6 Coupled Surge response of square TLP for Wave Height = 8 m and wave period = 10 sec.

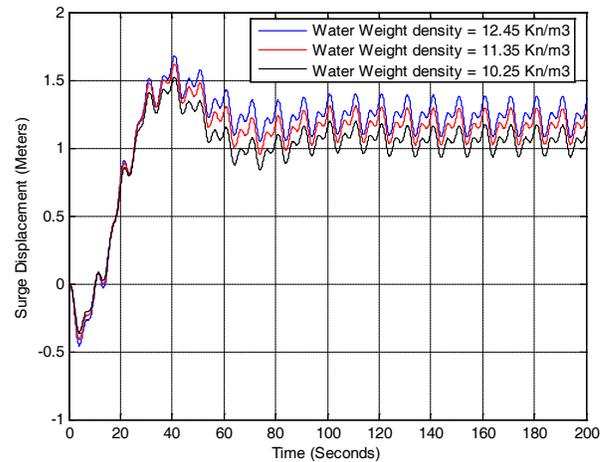


Fig. 7 Coupled Surge response of square TLP for Wave Height = 10 m and wave period = 10 sec.

B. Heave Response

The time histories are shown in Figs. 8 to 11. As expected, the response in the heave direction has very small values compared to that of the surge direction. This is attributed to the relatively high stiffness of the tethers in this direction together with the fact that the excitation is indirect in this case. Moreover, the heave response is inversely proportional to the wave period and directly proportional to wave height. The heave response appears to have a mean value of nearly zero. It is obvious that the increase of water density decrease slightly the amplitude of the heave response. Also, the transient state takes about 10-20 seconds where the stationary state begins and the motion is almost periodic.

It is interesting to note that, even both: the stiffness of TLP and the hydrodynamic force doesn't depend directly on water density in heave movement, the increase in water density leads to decrease in the drift value which increase the tether length, which affect indirectly the heave movement. Even the exciting hydraulic force is periodical sin wave the heave movement has more peaks value, illustrating higher

mode contribution in the response.

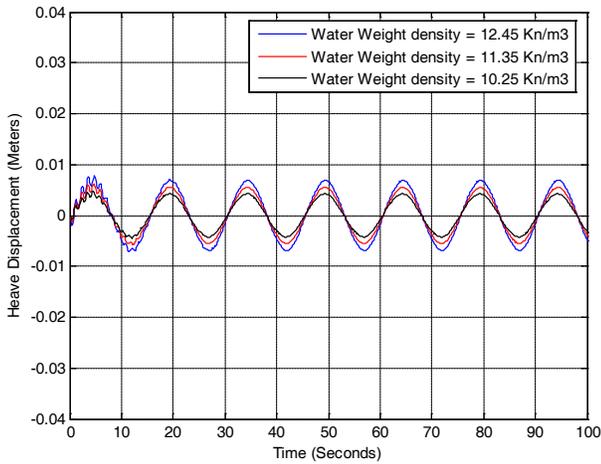


Fig. 8 Coupled Heave response of square TLP for Wave Height = 8 m and wave period = 15 sec.

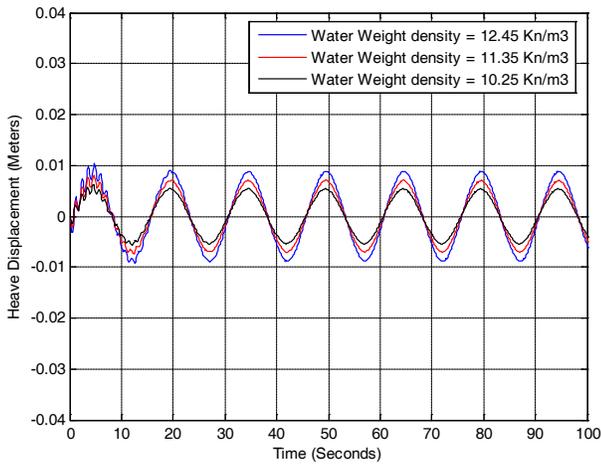


Fig. 9 Coupled Heave response of square TLP for Wave Height = 10 m and wave period = 15 sec

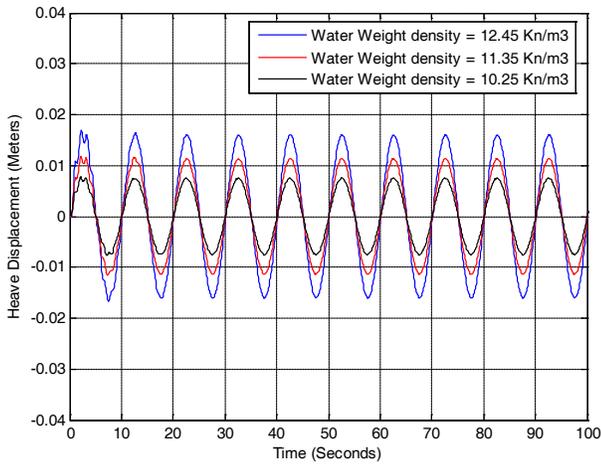


Fig. 10 Coupled Heave response of square TLP for Wave Height = 8 m and wave period = 10 sec

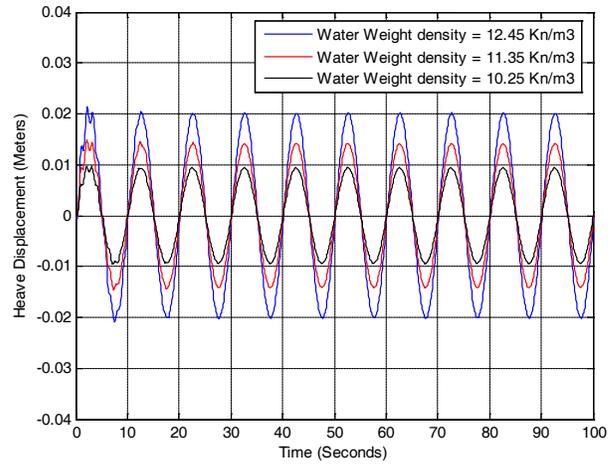


Fig. 11 Coupled Heave response of square TLP for Wave Height = 10 m and wave period = 10 sec

C. Pitch Response

The time histories shown in Figs. 12 to 15 it is clear that the increase of water density decrease the amplitude of the pitch response and that effect is more obvious for small wave period. Also the pitch response is inversely proportional to the wave period and directly proportional- but to a less extent- to wave height. The pitch response appears to have a mean value of nearly zero. Moreover, the transient state takes about 20-40 seconds before the stationary state begins.

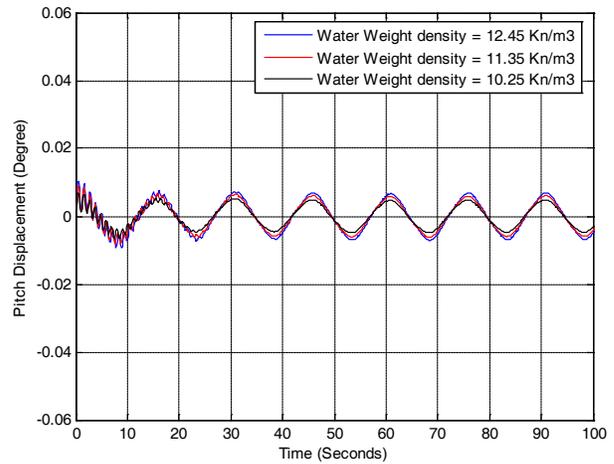


Fig. 12 Coupled Pitch response of square TLP for Wave Height = 8 m and wave period = 15 sec

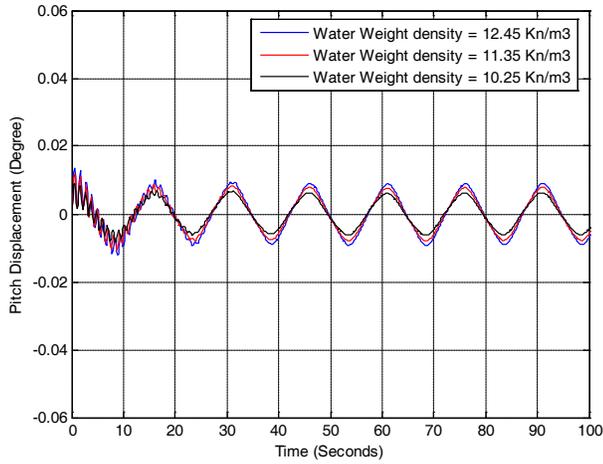


Fig. 13 Coupled Pitch response of square TLP for Wave Height = 10 m and wave period = 15 sec

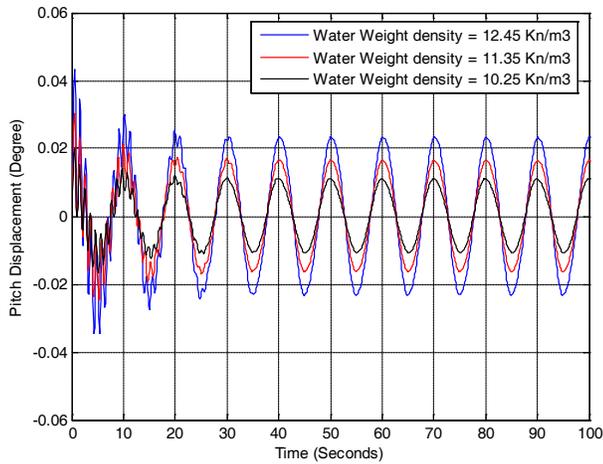


Fig. 14 Coupled Pitch response of square TLP for Wave Height = 8 m and wave period = 10 sec

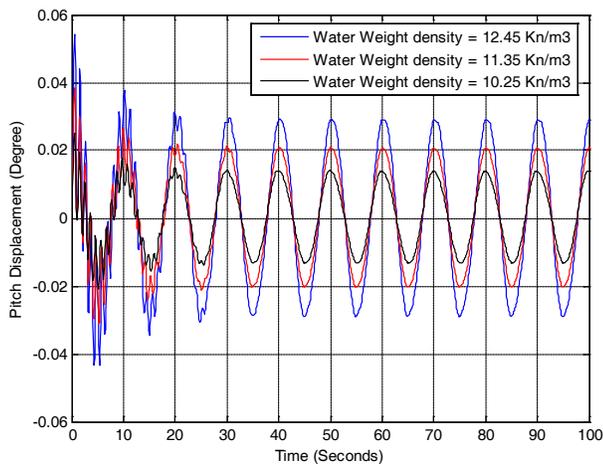


Fig. 15 Coupled Pitch response of square TLP for Wave Height = 10 m and wave period = 10 sec

D. Change in tether tension force

The time histories for the change in tether tension force for the square TLP are shown in Figs. 16 to 19.

It is noted that for small value of tether pretension the change in it is force is approximately 36% of it is initial force which may lead to fatigue failure, for big pretension force the ratio of change in force to it is initial value is about 10% so for same stress levels as pretension force reduced the probability of fatigue occurrence will increases.

For long wave period the change of tether tension force is not affected by the initial tether tension force as the magnitude of the tension change is slightly different.

For short wave period it can be observed that the permanent increase in tether tension force is higher for smaller initial tether tension force.

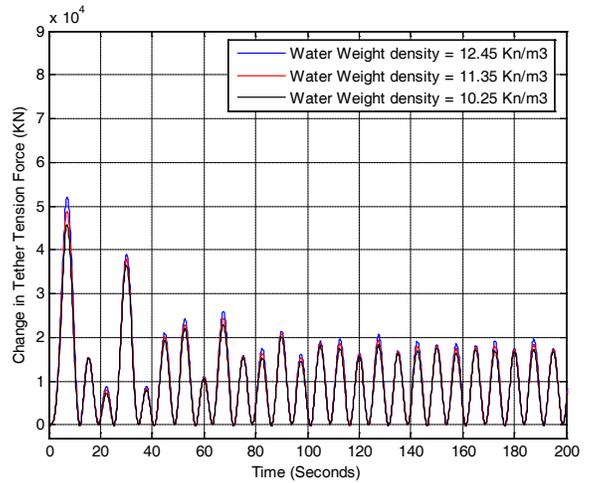


Fig. 16 Change in tether tension force of square TLP for Wave Height = 8 m and wave period = 15 sec

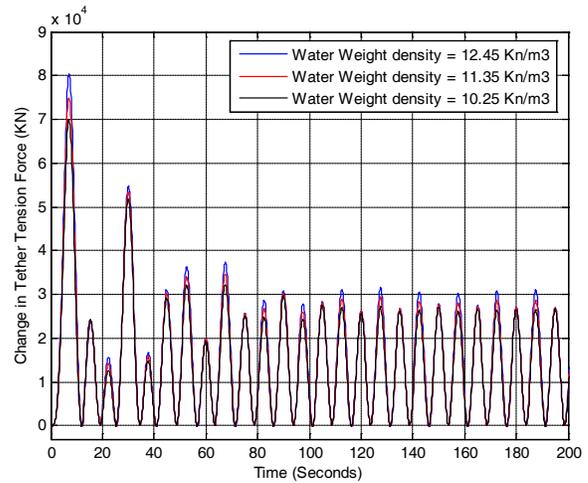


Fig. 17 Change in tether tension force of square TLP for Wave Height = 10 m and wave period = 15 sec

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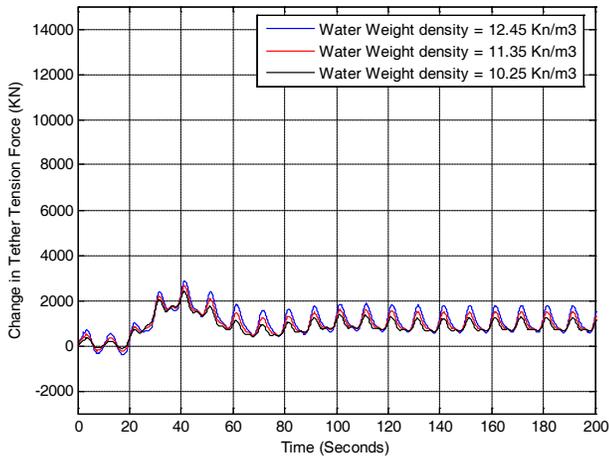


Fig. 18 Change in tether tension force of square TLP for Wave Height = 8 m and wave period = 10 sec

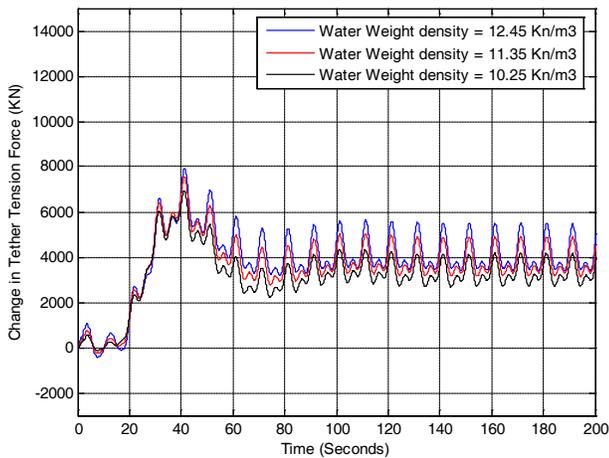


Fig. 19 Change in tether tension force of square TLP for Wave Height = 10 m and wave period = 10 sec

V. CONCLUSIONS

In this study a computer program was used to study the dynamics properties of square TLP, with concentration on the effect of water density the main conclusions were

1. The water density value effect the natural period for horizontal movement of square TLP while has little effect for vertical movements.
2. The water density value effect the amplitude of surge movement where, its effect on the amplitude of heave and pitch movements is less noticed.
3. The transition time for square TLP to reach a stable condition may reach up to 250 second.
4. For same stress level in tethers the change in tether tension force leading to probability of fatigue failure is more pronounced in short move periods and in small value of tether pretension force.